# Reuse, don't Recycle: Transforming Lock-free Algorithms that Throw Away Descriptors

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#### — Abstract -

In many lock-free algorithms, threads help one another, and each operation creates a *descriptor* that describes how other threads should help it. Allocating and reclaiming descriptors introduces significant space and time overhead. We introduce the first *descriptor* abstract data type (ADT), which captures the usage of descriptors by lock-free algorithms. We then develop a *weak descriptor* ADT which has weaker semantics, but can be implemented significantly more efficiently. We show how a large class of lock-free algorithms can be transformed to use weak descriptors, and demonstrate our technique by transforming several algorithms, including the leading *k*-compare-and-swap (*k*-CAS) algorithm. The original *k*-CAS algorithm allocates at least k + 1 new descriptors *per k-CAS*. In contrast, our implementation allocates two descriptors, and reductions of up to three orders of magnitude in peak memory usage.

1998 ACM Subject Classification D.1.3 [Programming Techniques]: Concurrent Programming

Keywords and phrases Concurrency, data structures, lock-free, synchronization, descriptors

Digital Object Identifier 10.4230/LIPIcs...

#### 1 Introduction

Many concurrent data structures use locks, but locks have downsides, such as susceptibility to convoying, deadlock and priority inversion. Lock-free data structures avoid these downsides, and can be quite efficient. They guarantee that some process will always makes progress, even if some processes halt unexpectedly. This guarantee is typically achieved with *helping*, which allows a process to harness any time that it would otherwise spend waiting for another operation to complete. Specifically, whenever a process p is prevented from making progress by another operation, it attempts to perform some (or all) of the work of the other operation, on behalf of the process that started it. This way, even if the other process has crashed, its operation can be completed, so that it no longer blocks p.

In simple lock-free data structures (e.g., [30, 16, 25, 28]), a process can determine how to help an operation that blocks it by inspecting a small part of the data structure. In more complex lock-free data structures [14, 19, 29, 10], processes publish *descriptors* for their operations, and helpers look at these descriptors to determine how to help. A descriptor typically encodes a sequence of steps that a process should follow in order to complete the operation that created it.

Since lock-free algorithms cannot use mutual exclusion, many helpers can simultaneously help an operation, potentially long after the operation has terminated. Thus, to avoid situations where helpers read inconsistent data in a descriptor and corrupt the data structure, each descriptor must remain consistent and accessible until no helper will ever access it again. This leads to *wasteful algorithms* which allocate a new descriptor for each operation.



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Leibniz International Proceedings in Informatics

LIPICS Schloss Dagstuhl – Leibniz-Zentrum für Informatik, Dagstuhl Publishing, Germany

In this work, we introduce two simple abstract data types (ADTs) that capture the way descriptors are used by wasteful algorithms (in Section 2). The *immutable descriptor* ADT provides two operations, *CreateNew* and *ReadField*, which respectively create and initialize a new descriptor, and read one of its fields. The *mutable descriptor* ADT extends the immutable descriptor ADT by adding two operations: *WriteField* and *CASField*. These allow a helper to modify fields of the descriptor (e.g., to indicate that the operation has been partially or fully completed). We also give examples of wasteful algorithms whose usage of descriptors is captured by these ADTs.

The natural way to implement the immutable and mutable descriptor ADTs is to have *CreateNew* allocate memory and initialize it, and to have *ReadField*, *WriteField* and *CAS-Field* perform a read, write and CAS, respectively. Every implementation of one of these ADTs must eventually reclaim the descriptors it allocates. Otherwise, the algorithm would eventually exhaust memory. We briefly explain why reclaiming descriptors is expensive.

In order to safely free a descriptor, a process must know that the descriptor is no longer *reachable*. This means no other process can reach the descriptor by following pointers in shared memory or in its private memory. State of the art lock-free memory reclamation algorithms such as hazard pointers [26] and DEBRA+ [7] can determine when no process has a pointer in its *private* memory to a given object, but they typically require the underlying algorithm to identify a time t after which the object is no longer reachable from *shared* memory. In an algorithm where each operation removes all pointers to its descriptor from shared memory, t is when O completes. However, in some algorithms (e.g., [11]), pointers to descriptors are "lazily" cleaned up by subsequent operations, so t may be difficult to identify. The overhead of reclaiming descriptors comes both from identifying t, and from actually running a lock-free memory reclamation algorithm.

Additionally, in some applications, such as embedded systems, it is important to have a small, predictable number of descriptors in the system. In such cases, one must use memory reclamation algorithms that aggressively reclaim memory to minimize the number of objects that are waiting to be reclaimed at any point in time. Such algorithms incur high overhead. For example, hazard pointers can be used to maintain a small memory footprint, but a process must perform costly memory fences *every* time it tries to access a new descriptor.

To circumvent the aforementioned problems, we introduce a weak descriptor ADT (in Section 3) that has slightly weaker semantics than the mutable descriptor ADT, but can be implemented without memory reclamation. The crucial difference is that each time a process invokes CreateNew to create a new descriptor, it invalidates all of its previous descriptors. An invocation of ReadField on an invalid descriptor fails and returns a special value  $\perp$ . Invocations of WriteField and CASField on invalid descriptors have no effect. We believe the weak descriptor ADT can be useful in designing new lock-free algorithms, since an invocation of ReadField that returns  $\perp$  can be used to inform a helper that it no longer needs to continue helping (making further accesses to the descriptor unnecessary).

We also identify a class of lock-free algorithms that use the descriptor ADT, and which can be *transformed* to use the weak descriptor ADT (in Section 3.2). At a high level, these are algorithms in which (1) each operation creates a descriptor and invokes a *Help* function on it, and (2) *ReadField*, *WriteField* and *CASField* operations occur only inside invocations of *Help*. Intuitively, the fact that these operations occur only in *Help* makes it easy to determine how the transformed algorithm should proceed when it performs an invalid operation: the operation being helped must have already terminated, so it no longer needs help. We prove correctness for our transformation, and demonstrate its use by transforming a wasteful implementation of a double-compare-single-swap (DCSS) primitive [17].

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We then present an extension to our weak descriptor ADT, and show how algorithms that perform *ReadField* operations *outside* of *Help* can be transformed to use this extension (in Section 4). We prove correctness for the transformation, and demonstrate its use by transforming wasteful implementations of a k-compare-and-swap (k-CAS) primitive [17] and the LLX and SCX primitives of Brown et al. [11]. These primitives can be used to implement a wide variety of advanced lock-free data structures. For example, LLX and SCX have been used to implement lists, chromatic trees, relaxed AVL trees, relaxed (a, b)-trees, relaxed b-slack trees and weak AVL trees [10, 8, 18].

We use mostly known techniques to produce an efficient, provably correct implementation of our extended weak descriptor ADT (in Section 5). The high level idea is to (1) store a sequence number in each descriptor, (2) replace pointers to descriptors with *tagged sequence numbers*, which contain a process name and a sequence number, and (3) increment the sequence number in a descriptor each time it is reused.

With this implementation, the transformed algorithms for k-CAS, and LLX and SCX, have some desirable properties. In the original k-CAS algorithm, each operation attempt allocates at least k+1 new descriptors. In contrast, the transformed algorithm allocates only two descriptors per process, once, at the beginning of the execution, and these descriptors are reused. Similarly, in the original algorithm for LLX and SCX, each SCX operation creates a new descriptor, but the transformed algorithm allocates only one descriptor per process, at the beginning of the execution and memory reclamation for descriptors (significantly reducing overhead), and results in an extremely small descriptor footprint.

We present extensive experiments on a 64-thread AMD system and a 48-thread Intel system (in Section 6). Our results show that transformed implementations always perform at least as well as their wasteful counterparts, and *significantly* outperform them in some workloads. In a k-CAS microbenchmark, our implementation outperformed wasteful implementations using fast distributed epoch-based reclamation [7], hazard pointers [26] and read-copy-update (RCU) [13] by up to 2.3x, 3.3x and 5.0x, respectively. In a microbenchmark using a binary search tree (BST) implemented with LLX and SCX, our transformed implementation is up to 57% faster than the next best wasteful implementation.

The crucial observation in this work is that, in algorithms where descriptors are used only to facilitate helping, a descriptor is no longer needed once its operation has terminated. This allows a process to reuse a descriptor as soon as its operation finishes, instead of allocating a new descriptor for each operation, and waiting considerably longer (and incurring much higher overhead) to reclaim it using standard memory reclamation techniques. The challenge in this work is to characterize the set of algorithms that can benefit from this observation, and to design and prove the correctness of a transformation that takes such algorithms and produces new algorithms that simply reuse a small number of descriptors. As a result of developing this transformation, we also produce significantly faster implementations of k-CAS, and LLX and SCX.

### 2 Wasteful Algorithms

In this section, we describe two classes of lock-free wasteful algorithms, and give descriptor ADTs that capture their behaviour. First, we consider algorithms with *immutable* descriptors, which are not changed after they are initialized. We then discuss algorithms with *mutable* descriptors, which are modified by helpers.

For the sake of illustration, we start by describing one common way that lock-free wasteful

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algorithms are implemented. Consider a lock-free algorithm that implements a set of *high-level* operations. Each high-level operation consists of one or more *attempts*, which either succeed, or fail due to contention. Each high-level operation attempt accesses a set of objects (e.g., individual memory locations or nodes of a tree). Conceptually, a high-level operation attempt locks a subset of these objects and then possibly modifies some of them. These locks are special: instead of providing exclusive access to a *process*, they provide exclusive access to a *high-level operation attempt*. Whenever a high-level operation attempt by a process p is unable to lock an object because it is already locked by another high-level operation attempt O, p first *helps* O to complete, before continuing its own attempt or starting a new one. By helping O complete, p effectively removes the locks that prevent it from making progress. Note that p is able to access objects locked for a different high-level operation attempt (which is not possible in traditional lock-based algorithms), but only for the purpose of helping the other high-level operation attempt complete.

We now discuss how helping is implemented. Each high-level operation or operation attempt allocates a new *descriptor* object, and fills it with information that describes any modifications it will perform. This information will be used by any processes that help the high-level operation attempt. For example, if the lock-free algorithm performs its modifications with a sequence of CAS steps, then the descriptor might contain the addresses, expected values and new values for the CAS steps.

A high-level operation attempt locks each object it would like to access by publishing pointers to its descriptor, typically using CAS. Each pointer may be published in a dedicated field for descriptor pointers, or in a memory location that is also used to store application values. For example, in the BST of Ellen et al., nodes have a separate field for descriptor pointers [14], but in Harris' implementation of multi-word CAS from single-word CAS, highlevel operations temporarily replace application values with pointers to descriptors [17].

When a process encounters a pointer ptr to a descriptor (for a high-level operation attempt that is not its own), it may decide to help the other high-level operation attempt by invoking a function Help(ptr). Typically, Help(ptr) is also invoked by the process that started the high-level operation. That is, the mechanism used to help is the same one used by a process to perform its own high-level operation attempt.

Wasteful algorithms typically assume that, whenever an operation attempt allocates a new descriptor, it uses fresh memory that has never previously been allocated. If this assumption is violated, then an *ABA problem* may occur. Suppose a process p reads an address x and sees A, then performs a CAS to change x from A to C, and interprets the success of the CAS to mean that x contained A at all times between the read and CAS. If another process changes x from A to B and back to A between p's read and CAS, then p's interpretation is invalid, and an ABA problem has occurred. Note that safe memory reclamation algorithms will reclaim a descriptor only if no process has, or can obtain, a pointer to it. Thus, no process can tell whether a descriptor is allocated fresh or reclaimed memory. So, safe memory reclamation will not introduce ABA problems.

#### 2.1 Immutable descriptors

We give a straightforward *immutable descriptor* ADT that captures the way that descriptors are used by the class of wasteful algorithms we just described. A *descriptor* has a set of fields, and each field contains a value. The ADT offers two operations: *CreateNew* and *ReadField*. *CreateNew* takes, as its arguments, a descriptor type and a sequence of values, one for each field of the descriptor. It returns a unique descriptor pointer *des* that has never previously been returned by *CreateNew*. Every descriptor pointer returned by *CreateNew* represents a

new immutable descriptor object. ReadField takes, as its arguments, a descriptor pointer des and a field f, and returns the value of f in des.

In wasteful algorithms, whenever a process wants to create a new descriptor, it simply invokes *CreateNew*. Whenever a helper wants to access a descriptor, it invokes *ReadField*.

#### 2.1.1 Progress

If the immutable descriptor ADT is implemented so that *CreateNew* allocates and initializes a new descriptor, and *ReadField* reads and returns a field of a descriptor, then its operations will be *wait-free* (i.e., each operation will terminate after a finite number of its own steps). However, wait-free descriptor operations are not necessary to guarantee lock-freedom for high-level operations that use descriptors. Instead, we simply require descriptor operations to be lock-free. We now explain why this is sufficient to implement lock-free data structures.

Consider a lock-free algorithm that uses a wait-free implementation of the immutable descriptor ADT. Suppose we transform this algorithm by replacing the wait-free implementation of the descriptor ADT with a *lock-free* implementation. We argue that the transformed algorithm remains lock-free. In other words, we show that, if processes take infinitely many steps in the transformed algorithm, then infinitely many high-level operations complete.

In the original algorithm, if processes take infinitely many steps, then infinitely many high-level operations will complete. The only steps we change to obtain the transformed algorithm are invocations of *CreateNew* and *ReadField*, some of which might no longer terminate. Therefore, the only way the transformed algorithm can *fail* to satisfy lock-freedom is if, eventually, all processes take steps only in non-terminating invocations of *CreateNew* and *ReadField*. (Otherwise, processes take infinitely many steps of the original algorithm, so infinitely many high-level operations will succeed.) In this case, only finitely many invocations of *CreateNew* and *ReadField* are lock-free, infinitely many invocations of *CreateNew* and/or *ReadField* must terminate. Thus, a lock-free implementation of the immutable descriptor ADT is sufficient to implement lock-free algorithms.

#### 2.1.2 Example Algorithm: DCSS

We use the double-compare single-swap (*DCSS*) algorithm of Harris et al. [17] as an example of a lock-free algorithm that fits the preceding description. Its usage of descriptors is easily captured by the immutable descriptor ADT. A  $DCSS(a_1, e_1, a_2, e_2, n_2)$  operation does the following *atomically*. It checks whether the values in addresses  $a_1$  and  $a_2$  are equal to a pair of expected values,  $e_1$  and  $e_2$ . If so, it stores the value  $n_2$  in  $a_2$  and returns  $e_2$ . Otherwise it returns the current value of  $a_2$ .

Pseudocode for the *DCSS* algorithm appears in Figure 1. At a high level, *DCSS* creates a descriptor, and then attempts to lock  $a_2$  by using CAS to replace the value in  $a_2$  with a pointer to its descriptor. Since the *DCSS* algorithm replaces values with descriptor pointers, it needs a way to distinguish between values and descriptor pointers (in order to determine when helping is needed). So, it steals a bit from each memory location and uses this bit to *flag* descriptor pointers.

We now give a more detailed description. DCSS starts by creating and initializing a new descriptor des at line 2. It then flags des at line 3. We call the result fdes a flagged pointer. DCSS then attempts to lock  $a_2$  in the loop at lines 4-7. In each iteration, it tries to store its flagged pointer in  $a_2$  using CAS. If the CAS is successful, then the operation attempt invokes DCSSHelp to complete the operation (at line 8). Now, suppose the CAS

1 2 3	$DCSS(a_1, e_1, a_2, e_2, n_2):$ $des := CreateNew(DCSSdes, a_1, e_1, a_2, e_2, n_2)$ fdes := flag(des)	17	$\begin{array}{l} \mathbf{type} \ DCSSdes: \\ \{ \mathrm{ADDR}_1, \mathrm{EXP}_1, \mathrm{ADDR}_2, \mathrm{EXP}_2, \mathrm{NEW}_2 \} \end{array}$
4	loop		
5	$r := CAS(a_2, e_2, fdes)$		
6	<b>if</b> $r$ is flagged <b>then</b> $DCSSHelp(r)$	21	DCSSHelp(fdes):
7	else exit loop	22	des := unflag(fdes)
8	if $r = e_2$ then $DCSSHelp(fdes)$	23	$a_1 := ReadField(des, ADDR_1)$
9	return r	24	$a_2 := ReadField(des, ADDR_2)$
		25	$e_1 := ReadField(des, EXP_1)$
11	DCSSRead(addr):	26	$\mathbf{if} \ *a_1 = e_1 \ \mathbf{then}$
12	loop	27	$n_2 := ReadField(des, NEW_2)$
13	r := *addr	28	$CAS(a_2, fdes, n_2)$
14	<b>if</b> $r$ is flagged <b>then</b> $DCSSHelp(r)$	29	else
15	else exit loop	30	$e_2 := ReadField(des, EXP_2)$
16	return r	31	$CAS(a_2, fdes, e_2)$

**Figure 1** Code for the *DCSS* algorithm of Harris et al. [17] using the *immutable descriptor* ADT.

fails. Then, the *DCSS* checks whether its CAS failed because  $a_2$  contained another *DCSS* operation's flagged pointer (at line 6). If so, it invokes *DCSSHelp* to help the other *DCSS* complete, and then retries its CAS. *DCSS* repeatedly performs its CAS (and helping) until the *DCSS* either succeeds, or fails because  $a_2$  did not contain  $e_2$ .

DCSSHelp takes a flagged pointer fdes as its argument, and begins by unflagging fdes (to obtain the actual descriptor pointer for the operation). Then, it reads  $a_1$  and checks whether it contains  $e_1$  (at line 26). If so, it uses CAS to change  $a_2$  from fdes to  $n_2$ , completing the DCSS (at line 28). Otherwise, it uses CAS to change  $a_2$  from fdes to  $e_2$ , effectively aborting the DCSS (at line 31). Note that this code is executed by the process that created the descriptor, and also possibly by several helpers. Some of these helpers may perform a CAS at line 26 and some may perform a CAS at line 28, but only the first of these CAS steps can succeed.

When a program uses DCSS, some addresses can contain either values or descriptor pointers. So, each read of such an address must be replaced with an invocation of a function called *DCSSRead*. *DCSSRead* takes an address *addr* as its argument, and begins by reading *addr* (at line 13). It then checks whether it read a descriptor pointer (at line 14) and, if so, invokes *DCSSHelp* to help that *DCSS* complete. *DCSSRead* repeatedly reads and performs helping until it sees a value, which it returns (at line 16).

#### 2.2 Mutable descriptors

In some more advanced lock-free algorithms, each descriptor also contains information about the *status* of its high-level operation attempt, and this status information is used to coordinate helping efforts between processes. Intuitively, the status information gives helpers some idea of what work has already been done, and what work remains to be done. Helpers use this information to direct their efforts, and update it as they make progress. For example, the state information might simply be a bit that is set (by the process that started the high-level operation, or a helper) once the high-level operation succeeds.

As another example, in an algorithm where high-level operation attempts proceed in several phases, the descriptor might store the current phase, which would be updated by helpers as they successfully complete phases. Observe that, since lock-free algorithms cannot use mutual exclusion, helpers often use CAS to avoid making conflicting changes to status information, which is quite expensive. Updating status information may introduce contention. Even when there is no contention, it adds overhead. Lock-free algorithms typically try to minimize updates to status information. Moreover, status information is usually simplistic, and is encoded using a small number of bits.

Status information might be represented as a single field in a descriptor, or it might be distributed across several fields. Any fields of a descriptor that contain status information are said to be *mutable*. All other fields are called *immutable*, because they do not change during an operation.

**Mutable descriptor ADT.** We now extend the immutable descriptor ADT to provide operations for changing (mutable) fields of descriptors. The *mutable descriptor* ADT offers four operations: *CreateNew*, *WriteField*, *CASField* and *ReadField*. The semantics for *CreateNew* and *ReadField* are the same as in the immutable descriptor ADT. *WriteField* takes, as its arguments, a descriptor pointer des, a field f and a value v. It stores v in field f of des. *CASField* takes, as its arguments, a descriptor pointer des, a field f, an expected value exp and a new value v. Let  $v_f$  be the value of f in des just before the *CASField*. If  $v_f = exp$ , then *CASField* stores v in f. *CASField* returns  $v_f$ . As in the immutable descriptor ADT, we require the operations of the mutable descriptor ADT to be lock-free.

#### 2.2.1 Example Algorithm: k-CAS

A k- $CAS(a_1, ..., a_k, e_1, ..., e_k, n_1, ..., n_k)$  operation atomically does the following. First, it checks if each address  $a_i$  contains its expected value  $e_i$ . If so, it writes a new value  $n_i$  to  $a_i$  for all i and returns true. Otherwise it returns false.

The k-CAS algorithm of Harris et al. [17] is an example of a lock-free algorithm that has descriptors with mutable fields. At a high level, a k-CAS operation O in this algorithm starts by creating a descriptor that contains its arguments. It then tries to lock each location  $a_i$  for the operation O by changing the contents of  $a_i$  from  $e_i$  to des, where des is a pointer to O's descriptor. If it successfully locks each location  $a_i$ , then it changes each  $a_i$  from des to  $n_i$ , and returns true. If it fails because  $a_i$  is locked for another operation, then it helps the other operation to complete (and unlock its addresses), and then tries again. If it fails because  $a_i$  contains an application value different from  $e_i$ , then the k-CAS fails, and unlocks each location  $a_j$  that it locked by changing it from des back to  $e_j$ , and returns false. (The same thing happens if O fails to lock  $a_i$  because the operation has already terminated.)

We now give a more detailed description of the algorithm. Pseudocode appears in Figure 2. A k-CAS operation creates its descriptor at line 5, and then invokes a function k-CASHelp to complete the operation. In addition to the arguments to its k-CAS operation, a k-CAS descriptor contains a 2-bit state field that initially contains Undecided and is changed to Succeeded or Failed depending on how the operation progresses. This state field is used to coordinate helpers.

Let p be a process performing (or helping) a k-CAS operation O that created a descriptor d. If p fails to lock some address  $a_i$  in d, then p attempts to change the *state* of d using CAS from *Undecided* to *Failed*. On the other hand, if p successfully locks each address in d, then p attempts to change the *state* of d using CAS from *Undecided* to *Succeeded*. Since the *state* field changes only from *Undecided* to either *Failed* or *Succeeded*, only the first CAS on the state field of d will succeed. The k-CAS implementation then uses a lock-free DCSS primitive (the one presented in Section 2.1.2) to ensure that p can lock addresses for O only while d's state is *Undecided*. This prevents helpers from erroneously performing successful CAS steps after the k-CAS operation is already over.

Recall that the DCSS algorithm allocates a descriptor for each DCSS operation. A k-CAS operation performs potentially many DCSS operations (at least k for a successful k-CAS), and also allocates its own k-CAS descriptor. The k-CAS algorithm need not be

```
type k-CASdes: {STATE, ADDR<sub>1</sub>, EXP<sub>1</sub>, NEW<sub>1</sub>,
 1
          ADDR_2, EXP_2, NEW_2, \ldots, ADDR_k, EXP_k, NEW_k
    \triangleright k-CAS ADT operations
 3
    k-CAS(a_1, e_1, n_1, a_2, e_2, n_2, \dots, a_k, e_k, n_k):
4
       des := CreateNew(k-CASdes, Undecided, a_1, e_1, n_1, \ldots)
 \mathbf{5}
        fdes := flagged version of des
 6
        return k-CASHelp(fdes)
 7
    k-CASRead(addr):
9
       loop
10
          r := DCSSRead(addr)
11
           if r is flagged then k-CASHelp(r)
12
           else exit loop
13
        return r
14
    ▷ Private procedures
16
    k-CASHelp(fdes)
17
       des := remove the flag from fdes
18
       \triangleright Use DCSS to store fdes in each of a_1, a_2, \ldots, a_k
19
       \triangleright only if des has STATE Undecided and a_i = e_i for all i
20
        if ReadField(des, STATE) = Undecided then
21
           state := Succeeded
^{22}
           for i = 1...k do
23
    retry\_entry:
^{24}
             a_1 := ReadField(des, STATE)
25
             a_2 := ReadField(des, ADDR_i)
26
              e_2 := ReadField(des, EXP_i)
27
              val := DCSS(\langle des, STATE \rangle, Undecided, a_2, e_2, fdes)
^{28}
              if val is flagged then
29
                 if val \neq fdes then
30
                    k-CASHelp(val)
^{31}
^{32}
                    goto retry_entry
              else
33
34
                 if val \neq e_2 then
                    state := Failed
35
                    break
36
           CASField(des, STATE, Undecided, state)
37
       \triangleright Replace fdes in a_1, ..., a_k with n_1, ..., n_k or e_1, ..., e_k
39
        state := ReadField(des, STATE)
40
        for i = 1...k do
^{41}
          a = ReadField(des, ADDR_i)
42
           if state = Succeeded then
^{43}
             new := ReadField(des, NEW_i)
44
           else
45
              new := ReadField(des, EXP_i)
46
           CAS(a, fdes, new)
47
        return (state = Succeeded)
^{48}
```

**Figure 2** Code for the *k*-CAS algorithm of Harris et al. [17] using the *mutable descriptor* ADT.

aware of DCSS descriptors (or of the bit reserved in each memory location by the DCSS algorithm to flag values as DCSS descriptor pointers), since it can simply use the *DCSSRead* procedure described above whenever it accesses a memory location that might contain a DCSS descriptor. However, the k-CAS algorithm performs DCSS on the *state* field of a k-CAS descriptor, which is accessed using the k-CAS descriptor's *ReadField* operation. To allow DCSS to access the *state* field, we must modify DCSS slightly. First, instead of passing an address  $a_1$  to DCSS, we pass a pointer to the k-CAS descriptor and the name of the *state* field (at line 28 of Figure 2). Second, we replace the read of  $addr_1$  in DCSS (at line 26 of Figure 1) with an invocation of *ReadField*.

Since k-CAS descriptor pointers are temporarily stored in memory locations that normally contain application values, the k-CAS algorithm needs a way to determine whether a value in a memory location is an application value or a k-CAS descriptor pointer. In the DCSS algorithm, the solution was to reserve a bit in each memory location, and use this bit to *flag* the value contained in the location as a pointer to a DCSS descriptor. Similarly, the k-CAS algorithm reserves a bit in each memory location to flag a value as a k-CAS descriptor pointer. The k-CAS and DCSS algorithms need not be aware of each other's reserved bits, but they should not reserve the same bit (or else, for example, a DCSS operation could encounter a k-CAS descriptor pointer, and interpret it as a DCSS descriptor pointer).

When the k-CAS algorithm is used, some memory addresses may contain either values or descriptor pointers, so reads of such addresses must be replaced by a k-CASRead operation. This operation reads an address, and checks whether it contains a k-CAS descriptor pointer. If so, it helps the k-CAS operation to complete, and tries again. Otherwise, it returns the value it read. For further details, on the k-CAS algorithm refer to [17].

#### 3 Weak descriptors

In this section we present a *weak descriptor* ADT that has weaker semantics than the mutable descriptor ADT, but can be implemented more efficiently (in particular, without requiring any memory reclamation for descriptors). We identify a class of algorithms that use the mutable descriptor ADT, and which can be transformed to use the weak descriptor ADT, instead.

We first discuss a restricted case where operation attempts only create a single descriptor, and we give an ADT, transformation and proof for that restricted case. (In the next section, we describe how the ADT and transformation can be modified slightly to support operation attempts that create multiple descriptors.)

### 3.1 Weak descriptor ADT

The weak descriptor ADT is a variant of the mutable descriptor ADT that allows some operations to *fail*. To facilitate the discussion, we introduce the concept of descriptor validity. Let *des* be a pointer returned by a *CreateNew* operation O by a process p, and d be the descriptor pointed to by *des*. In each configuration, d is either **valid** or **invalid**. Initially, d is valid. If p performs another *CreateNew* operation O' after O, then d becomes invalid immediately after O' (and will never be valid again).

We say that a ReadField(des,...), WriteField(des,...) or CASField(des,...) operation is performed **on a descriptor** d, where des is a pointer to d. An operation on a valid (resp., invalid) descriptor is said to be valid (resp., invalid). Invalid operations have no effect on any base object, and return a special value  $\perp$  (which is never contained in a field of any descriptor) instead of their usual return value. We say that a *CreateNew* operation O is performed **on a descriptor** d if O returns a pointer to d. Observe that a *CreateNew* operation is always valid. We say that a process p **owns** a descriptor d if it performed a *CreateNew* operation that returned a pointer des to d.

The semantics for *CreateNew* are the same as in the mutable descriptor ADT. The semantics for the other three operations are the same as in the mutable descriptor ADT, except that they can be invalid. As in the previous ADTs, these operations must be lock-free.

#### 3.2 Transforming a class of algorithms to use the weak descriptor ADT

We now formally define a class of lock-free algorithms that use the mutable descriptor ADT, and can easily be transformed so that they use the weak descriptor ADT, instead. We say that a step s of an execution is *nontrivial* if it changes the state of an object o in shared memory, and *trivial* otherwise. In particular, all invalid operations are trivial, and an unsuccessful CAS or a CAS whose expected and new values are the same are both trivial. In the following, we abuse notation slightly by referring interchangeably to a descriptor and a pointer to it.

▶ **Definition 1.** Weak-compatible algorithms (WCA) are lock-free wasteful algorithms that use the mutable descriptor ADT, and have the following properties:

- 1. Each high-level operation attempt O by a process p may create (and initialize) a single descriptor d. Inside O, p may perform at most one invocation of a function Help(d) (and p may not invoke Help(d) outside of O).
- 2. A process may help any operation attempt O' by another process by invoking Help(d') where d' is the descriptor that was created by O'.
- **3.** If O terminates at time t, then any steps taken in an invocation of Help(d) after time t are trivial (i.e., do not change the state of any shared object, incl. d).
- 4. While a process  $q \neq p$  is performing Help(d), q cannot change any variables in its private memory that are still defined once Help(d) terminates (i.e., variables that are local to the process q, but are not local to Help).
- 5. All accesses (read, write or CAS) to a field of d occur inside either Help(d) or O.

At a high level, properties 1 and 2 of WCA describe how descriptors are created and helped. Property 4 intuitively states that, whenever a process q finishes helping another process perform its operation attempt, q knows only that it finished helping, and does not remember anything about what it did while helping the other process. In particular, this means that q cannot pay attention to the return value of *Help*. We explain why this behaviour makes sense. If q creates a descriptor d as part of a high-level operation attempt O and invokes Help(d), then q might care about the return value of Help, since it needs to compute the response of O. However, if q is just helping another process p's high-level operation attempt O, then it does not care about the response of Help, since it does not need to compute the response of O. The remaining properties, 3 and 5, allow us to argue that the contents of a descriptor are no longer needed once the operation that created it has terminated (and, hence, it makes sense for the descriptor to become invalid). In Section 4, we will study a larger class of algorithms with a weaker version of property 5.

**The transformation.** Each algorithm in WCA can be transformed in a straightforward way into an algorithm that uses the weak descriptor ADT as follows. Consider any *ReadField* or *CASField* operation *op* performed by a high-level operation attempt O in an invocation of Help(d), where d was created by a *different* high-level operation attempt O'. Note that *op* is performed while O is *helping* O'. After *op*, a check is added to determine whether *op* was invalid, in which case p returns from Help immediately. (In this case, Help does not need to continue, since *op* will be invalid only if O' has already been completed by the process that owns d or a helper.)

**Example Algorithm: DCSS.** Figure 3 shows code for the *DCSS* algorithm in Figure 1 that has been *transformed* to use the weak descriptor ADT. There, we include only the *DCSSHelp* procedure, since it is the only one that differs from Figure 1. The transformation adds lines 4, 6, 8, 11 and 15 to *check* whether the preceding invocations of *ReadField* are invalid.

1	DCSSHelp(fdes):
2	des := Unflag(fdes)
3	$a_1 := ReadField(des, ADDR_1)$
4	if $a_1 = \bot$ then return
5	$a_2 := ReadField(des, ADDR_2)$
6	if $a_2 = \bot$ then return
7	$e_1 := ReadField(des, EXP_1)$
8	if $e_1 = \bot$ then return
9	$\mathbf{if} \ *a_1 = e_1 \ \mathbf{then}$
10	$n_2 := ReadField(des, NEW_2)$
11	if $n_2 = \bot$ then return
12	$CAS(a_2, fdes, n_2)$
13	else
14	$e_2 := ReadField(des, EXP_2)$
15	if $e_2 = \bot$ then return
16	$CAS(a_2, fdes, e_2)$

**Figure 3** Applying the transformation to *DCSS*.

#### 3.3 Correctness

We argue that our transformation takes a linearizable algorithm  $\mathcal{A} \in WCA$  that uses mutable descriptors and produces a linearizable algorithm  $\mathcal{A}'$  that uses weak descriptors. Consider any execution e' of the transformed algorithm  $\mathcal{A}'$ . We prove there exists an execution e of the original algorithm  $\mathcal{A}$  that performs the same high-level operations, in the same order, and with the same responses, as in e'. We explain how this helps. Since e is a correct execution of the original algorithm  $\mathcal{A}$ , the high-level operations performed in e must respect the sequential specification(s) of the object(s) implemented in  $\mathcal{A}$ . Furthermore, since e'performs the same high-level operations, in the same order, and with the same responses, the high-level operations in e' must also respect the sequential specification(s) of the same object(s). Therefore, the transformed algorithm  $\mathcal{A}'$  is correct.

We construct e as follows. By Property 5 of WCA, all *ReadField*, *WriteField* and *CAS*-*Field* operations occur in *Help*. Whenever a check by a process p follows a *ReadField* or *CASField* in e' that returns  $\perp$  (because the operation attempt O being helped by p has already terminated), we replace that check by a consecutive sequence of steps in which p finishes its invocation of *Help*. All other checks immediately following *ReadField* or *CASField* are simply removed.

By Property 3 of WCA, none of the steps added to e change the state of any shared object. So, these steps will not change the behaviour of any other process. We also argue that none of these steps make any changes to p's private memory that persist after p finishes its invocation of Help. (I.e., any changes these steps make to p's private memory are *reverted* by the time p finishes its invocation of Help, so p's private memory is the same just after the invocation of Help as it was just before the invocation of Help.) So, these steps will not change the behaviour of p after it finishes its invocation of Help. Observe that, whenever a process performs a *ReadField* or *CASField* operation on a descriptor that it created, this operation will return a value different from  $\perp$ . This is due to Property 1 of WCA, and the definition of the weak descriptor ADT, which states that d becomes invalid only after O has terminated. Since p's invocation of *ReadField* or *CASField* returns  $\perp$ , p must therefore be performing Help(d) where d was created by a *different* process. Thus, Property 4 of WCA implies that, after p performs the sequence of steps to finish its invocation of Help(d), its private memory has the same state as it did just before it invoked Help.

```
DCSSHelp(fdes):
 1
        des := Unflag(fdes)
2
        values := ReadImmutables(des)
3
        if values = \bot then return
 4
        \langle a_1, e_1, a_2, e_2, n_2 \rangle := values
 5
        if *a_1 = e_1 then
 7
           CAS(a_2, fdes, n_2)
 8
        else
9
           CAS(a_2, fdes, e_2)
10
```

**Figure 4** Using *ReadImmutables* to optimize and streamline the transformed DCSS algorithm.

#### 3.4 Reading immutable fields efficiently

If an invocation of Help(des) accesses many immutable fields of a descriptor, then we can optimize it by replacing many *ReadField* operations with a single, more efficient operation called *ReadImmutables*. This operation reads and returns *all* of a descriptor's immutable fields, unless the descriptor is invalid, in which case it returns  $\perp$ .

To use ReadImmutables in Help(des), one can simply perform, at the beginning of Help, a ReadImmutables operation, followed by an *if*-statement that checks whether it the operation invalid, and, if so, returns immediately. Then, in the body of Help(des), each invocation of ReadField(des, f), where f is immutable, is replaced with a direct read from the set of values returned by ReadImmutables. We demonstrate this approach on the transformed pseudocode for DCSS in Figure 3. Figure 4 shows the result. Since all fields of a DCSS descriptor are immutable, *every* invocation of ReadField can be replaced with a direct read from the result of the ReadImmutables operation performed at line 3. (This will not be the case in an algorithm where the Help procedure reads mutable fields.) Since ReadImmutables replaces several invocations of ReadField, it has the added benefit of making code simpler and shorter.

#### 4 Extended Weak Descriptors

In this section, we describe an extended version of the weak descriptor ADT, and an extended version of the transformation in Section 3.2. This extended transformation weakens property 5 of WCA so that *ReadField* operations on a descriptor d can also be performed *outside* of Help(d). At a high level, we handle *ReadField* operations performed outside of *Help* as follows. For *ReadFields* performed inside *Help*, we have seen that we can simply stop helping when  $\perp$  is returned. However, for *ReadFields* performed outside of *Help*, it is not clear, in general, how we should respond if  $\perp$  is returned. Intuitively, the goal is to find a value that *ReadField* can return so that the algorithm will behave the same way as it would if the descriptor were still valid. In some algorithms, just knowing that an operation has been completed gives us enough information to determine what a *ReadField* operation should return (as we will see below).

**Extended weak descriptor ADT.** This ADT is the same as the weak descriptor ADT, except that *ReadField* is extended to take, as an additional argument, a default value dv that is returned instead of  $\perp$  when the operation is invalid. Observe that the weak descriptor ADT is a special case of the extended weak descriptor ADT where each argument dv to an invocation of *ReadField* is  $\perp$ .

The extended transformation. CASField and WriteField operations are handled the same way as in the WCA transformation. However, an invocation of ReadField(des, f) is

handled differently depending on whether it occurs inside an invocation of Help(des). If it does, it is replaced with an invocation of  $ReadField(des, f, \perp)$  followed by the check, as in the WCA transformation. If not, it is replaced with an invocation of ReadField(des, f, dv), where the choice of dv is specific to the algorithm being transformed.

Let  $\mathcal{A}$  be any algorithm that uses mutable descriptors, and satisfies properties 1-4 of WCA algorithms (see Definition 1), as well as a weaker version of property 5, called property 5', which states: every write or CAS to a field of a descriptor d must occur in an invocation of Help(d). Let e be an execution of  $\mathcal{A}$  and let e' be an execution that is the same as e, except that one (arbitrary) descriptor d becomes invalid at some point t after the high-level operation attempt O that created d terminates. (When we say that d becomes invalid at time t, we mean that after t, each invocation of ReadField(d, f, dv) that is performed outside of Help(d) returns its default value dv.)

Let O' be any high-level operation attempt in e' which, after t, performs ReadField on d outside of Help(d). We say that an extended transformation is correct for  $\mathcal{A}$  if, for all choices of e, e', d, t, and O', the exact same changes are performed by O' in e and e' to any variables that are still defined once O' terminates (i.e., variables that are local to the process performing O', but are not local to O', and variables in shared memory), and O' returns the same response in both executions. An algorithm  $\mathcal{A}$  is an extended weak-compatible algorithm (and is in the class EWCA) if there is an extended transformation that is correct for  $\mathcal{A}$ .

#### 4.1 Correctness

Consider any extended transformation which is correct for a linearizable algorithm  $\mathcal{A}$  that uses mutable descriptors. We prove the result of applying this transformation to  $\mathcal{A}$  is a linearizable algorithm  $\mathcal{A}'$  that uses extended weak descriptors. Specifically, let e' be any execution of  $\mathcal{A}'$ . We prove there is an execution e of  $\mathcal{A}$  that performs the same high-level operations, in the same order, with the same responses, as in e'.

First, we define an execution  $e_0$ . Whenever a check in e' by a process p in Help(d) determines that the preceding *ReadField* or *CASField* on a descriptor d is *invalid* (which means that the operation attempt being helped by p has already terminated), we replace that check by a consecutive sequence of steps in which p finishes its invocation of Help(d). By Property 3 of WCA, none of these added steps change the state of any shared variable. Moreover, by Property 4 of WCA, p does not change any variable that is still defined after its invocation of Help, so p has the same local state after Help in  $e_0$  and e'. Whenever such a check determines that the preceding *ReadField* or *CASField* is *valid*, we simply remove this check. Observe that each invalid operation in  $e_0$  is an invalid *ReadField* operation on some descriptor d performed outside of Help(d).

Let  $d_1, d_2, ...$  be the sequence of descriptors created in  $e_0$ . We inductively construct a sequence  $e_1, e_2, ...$  of executions such that  $e_i$  differs from  $e_{i-1}$  only in that descriptor  $d_i$  never becomes invalid in  $e_i$ . Specifically, for each high-level operation attempt O' that performs an invalid *ReadField* operation on descriptor  $d_i$  outside of  $Help(d_i)$ , consider the first such *ReadField* operation R. All of the steps of O' prior to R are the same in  $e_i$  as in  $e_{i-1}$ . After R, O' continues to take steps in  $e_i$ , but each *ReadField* operation that O' performs on a field f of  $d_i$  returns the contents of f (instead of a default value). This may result in O' executing completely different code paths in  $e_{i-1}$  and  $e_i$ . However, by the definition of an extended transformation that is correct for  $\mathcal{A}$ , O' returns the same response in  $e_i$ and  $e_{i-1}$  and performs the *exact same changes* to any variables that are still defined once O' terminates. Thus, for each variable v that is still defined once O' terminates, we can schedule the sequence of changes to v in the exact same way in  $e_i$  and  $e_{i-1}$  (which implies that any reads in  $e_{i-1}$  which see these changes can be scheduled appropriately in  $e_i$ ).

Since the claim holds for all i, there is an execution e in which no descriptor becomes invalid (so e is an execution of  $\mathcal{A}$ ), and the same high-level operation attempts are performed, in the same order, and with the same responses.

#### 4.2 Multiple descriptors per operation attempt

In some lock-free algorithms, a high-level operation attempt can create several different descriptors, and potentially invoke a different *Help* procedure for each descriptor. We describe how to adjust the definitions above to support these kinds of algorithms. For simplicity, we think of there being a single *Help* procedure that checks the type of the descriptor passed to it, and behaves differently for different types.

In order to allow a high-level operation attempt to create multiple descriptors without simply invalidating the ones it previously created, we update the definition of valid and invalid descriptors. Let des be a pointer to a descriptor d of type T returned by a CreateNew operation C performed by process p. Initially, d is valid. If p performs another CreateNew operation C' with the same descriptor type T after C, then d becomes invalid immediately after C' (and will never be valid again).

With this definition of valid and invalid descriptors, it might initially seem like an operation cannot create multiple descriptors of the same type T. However, this turns out not to be a problem. If an operation should create multiple descriptors of type T, we can simply imagine creating multiple *clone* types  $T_1, T_2, ...$  that have the exact same fields as T. To create k descriptors of type T, one would then create k clone types, and have an operation invoke *CreateNew* once for each clone type. (However, we are unaware of any algorithms in which a high-level operation attempt creates multiple descriptors of the same type.)

We also slightly modify Property 1 of (extended) weak-compatible algorithms, as follows, to accommodate the use of multiple descriptors. Each high-level operation attempt O by a process p may create (and initialize) a sequence D of descriptors, each with a **unique type**. Inside O, p may perform at most one invocation of a function Help(d) for each  $d \in D$  (and p may not invoke Help(d) outside of O). Note that the proof for the extended weak transformation goes through unchanged.

#### 4.3 Example Algorithm: k-CAS

In this section, we explain how the extended transformation is applied to the k-CAS algorithm presented in Section 2.2.1. Note that no invocations of *ReadField* on a DCSS descriptor *des* are performed outside of HelpDCSS(des). There is only one place in the algorithm where an invocation I of *ReadField* on a k-CAS descriptor *des* is performed *outside* of Help(des) (the *Help* procedure for k-CAS). Specifically, I reads the *state* field of a k-CAS descriptor inside the modified version of HelpDCSS. Recall that the k-CAS algorithm passes a k-CAS descriptor pointer and the name of the *state* field as the first argument to DCSS at line 28 of Figure 2, and the DCSS algorithm is modified to use *ReadField* at line 26 of Figure 1 to read this *state* field. We choose the default value dv = Succeeded for this invocation of *ReadField*. We explain why this extended transformation of the k-CAS algorithm

When I is performed at line 26 of DCSSHelp (in Figure 1), its response is compared with  $e_1$ , which contains Undecided. If I returns Undecided, then the CAS at line 28 is performed, and the process p performing I returns from HelpDCSS. Otherwise, the CAS at line 31 is performed, and p returns from HelpDCSS.

Suppose I is invalid. Then, we know the k-CAS operation attempt that created des has been completed. We use the following algorithm specific knowledge. After a k-CAS operation attempt has completed, its k-CAS descriptor has state Succeeded or Failed (and is never changed back to Undecided). (This can be determined by inspection of the code.) Thus, if I were valid, its response would not be Undecided, and p would perform the CAS at line 31 and return from HelpDCSS. Since dv = Succeeded, p does exactly the same thing when I is invalid. (Note that the exact value of state is unimportant. It is only important that it is not Undecided.)

#### 4.4 Example Algorithm: LLX and SCX

In this section, we explain how the extended transformation is applied to the multiword synchronization primitives load-linked-extended (LLX) and store-conditional-extended (SCX) of Brown et al. [11]. Note that Brown et al. [10] also used these primitives to design a tree update template that can be followed to produce a fast lock-free implementation of any data structure based on a down-tree (a directed acyclic graph where each node has indegree one). Thus, by optimizing LLX and SCX, we also optimize the tree update template, and all of the data structures that have been implemented with it. Pseudocode for LLX and SCX using mutable descriptors is presented in Figure 5.

LLX and SCX operate on multi-field *data records*, which can be used to represent, e.g., nodes in a tree, or records in a table. Like descriptors, *data records* contain mutable and immutable fields. However, whereas descriptors are used only to facilitate helping, and are not part of a sequential data structure, data records are.

LLX(r) attempts to take a snapshot of the mutable fields of a Data-record r. If it is concurrent with an SCX involving r, it may return FAIL, instead. Individual fields of a Data-record can also be read directly. An SCX(V, R, fld, new) takes as its arguments a sequence V of Data-records, a subsequence R of V, a pointer fld to a mutable field of one Data-record in V, and a new value new for that field. The SCX tries to atomically: store the value new in the field that fld points to and finalize each Data-record in R. Once a Data-record is finalized, its mutable fields cannot be changed by any subsequent SCX, and any LLX of the Data-record will return FINALIZED instead of a snapshot.

Before a process invokes SCX, it must perform an LLX(r) on each Data-record r in V. The last such LLX by the process is said to be *linked* to the SCX, and the linked LLXmust return a snapshot of r (not FAIL or FINALIZED). An SCX(V, R, fld, new) by a process modifies the data structure and returns TRUE only if no Data-record r in V has changed since its linked LLX(r); otherwise the SCX fails and returns FALSE. Although LLX and SCX can fail, their failures are limited in such a way that they can be used to build data structures with lock-free progress. See [11] for a more formal specification of these primitives.

Each SCX operation creates a new descriptor called an SCX-record. LLX and SCX requires each Data-record r to have a dedicated field r.des that stores a pointer to an SCX-record, and this field is only ever accessed by LLX and SCX operations. Each Data-record also has a marked bit which is accessed only by LLX and SCX. This field is used by SCX to finalize Data-records. We say that a Data-record is marked if its marked bit is set. SCX-records have two mutable fields: a 2-bit state field and an allFrozen bit. The state field contains one of three values: InProgress, Committed and Aborted.

The following properties of the LLX and SCX algorithm are relevant for our purposes.

P1. Before the first invocation of Help(des) for an SCX O (performed by O or a helper) has been completed, the SCX-record des created by O has its *state* field set to *Committed* or *Aborted*, and, after this, the *state* field of des is never changed again.

## XX:16 Reuse, don't Recycle: Transforming Lock-free Algorithms that Throw Away Descriptors

type SCXdes		
Immutable descr		
NFREEZE	▷ number of Data-records to be frozen	
NFINALIZE	▷ number of Data-records to be finalized	
$V_1, V_2,$	▷ Data-records to be frozen	
$R_1, R_2,$	$\triangleright$ Data-records to be finalized (must be a subsequence of $\langle V \rangle$	$(1, V_2, \ldots))$
$DES_1, DES_2, \dots$	$\triangleright$ descriptor pointers read from V <sub>1</sub> . <i>info</i> , V <sub>2</sub> . <i>info</i> ,	
FLD	$\triangleright$ pointer to a field of some V <sub>i</sub>	
NEW	▷ value to be written into the field FLD	
OLD	▷ value previously read from the field FLD	
▷ Mutable descrip		
STATE	▷ one of {InProgress, Committed, Aborted}	
ALLFROZEN	⊳ Boolean	
LLX(r) by process $p$		
$marked_1 := r.marked_1$	ked	
rinfo := r.info		
	d(SCXdes, rinfo, STATE)	
$marked_2 := r.marked_2$		
	ed or $(state = Committed and not marked_2)$ then	$\triangleright$ if <i>r</i> was not frozen at line 4
	<i>r.m.</i> and record the values in local variables $m_1,, m_y$	$\sim$ 117 was not 1102cm at 1111e 4
		N if winto contains the same
<b>if</b> $r.info = rin$		$\triangleright$ if <i>r.info</i> contains the same
	$p, \langle m_1,, m_y \rangle \rangle$ in <i>p</i> 's local table	▷ descriptor as on line 3
return (n	$m_1, \ldots, m_y$	
<b>if</b> $state = InProperty$	gress <b>then</b> Help(rinfo)	
	en return Finalized	
else return		
> Preconditions: (1) f	$V_k \rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new)$ by process <i>p</i> for each <i>r</i> in <i>V</i> , <i>p</i> has performed an invocation <i>I<sub>r</sub></i> of <i>LLX</i> ( <i>r</i> ) linked (2) <i>new</i> is not the initial value of <i>fld</i> (3) for each <i>r</i> in <i>V</i> , no <i>SCX</i> ( <i>V'</i> , <i>R'</i> , <i>fld</i> , <i>new</i> ) was linearized before <i>des<sub>k</sub></i> be the descriptor pointers for <i>V</i> <sub>1</sub> , <i>V</i> <sub>2</sub> ,, <i>V<sub>k</sub></i> in <i>p</i> 's local table of the for <i>fld</i> stored in <i>p</i> 's local table of <i>LLX</i> results	$I_r$ was linearized
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the valu des := CreateNew $(R_1, R_1), (R_2)$ (FLD, fld), (	$V_k\rangle$ , $R = \langle R_1, R_2,, R_l \rangle$ , $fld$ , $new$ ) by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) $new$ is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results ( $SCXdes$ , {(NFREEZE, $k$ ), (NFINALIZE, $l$ ), ( $V_1, V_1$ ), ( $V_2, V_2$ ),, $v_r R_2$ ),, ( $R_l, R_l$ ), (DES <sub>1</sub> , $des_1$ ), (DES <sub>2</sub> , $des_2$ ),, (DES <sub>k</sub> , $des_k$ ), (NEW, $new$ ), (OLD, $old$ ), (STATE, InProgress), (ALLFROZEN, $Fd$	$I_r$ was linearized f <i>LLX</i> results $(V_k, V_k),$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the valu des := CreateNew $(R_1, R_1), (R_2)$	$V_k\rangle$ , $R = \langle R_1, R_2,, R_l \rangle$ , $fld$ , $new$ ) by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) $new$ is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results ( $SCXdes$ , {(NFREEZE, $k$ ), (NFINALIZE, $l$ ), ( $V_1, V_1$ ), ( $V_2, V_2$ ),, $v_r R_2$ ),, ( $R_l, R_l$ ), (DES <sub>1</sub> , $des_1$ ), (DES <sub>2</sub> , $des_2$ ),, (DES <sub>k</sub> , $des_k$ ), (NEW, $new$ ), (OLD, $old$ ), (STATE, InProgress), (ALLFROZEN, $Fd$	$I_r$ was linearized f <i>LLX</i> results $(V_k, V_k),$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), return $Help(des)$	$V_k\rangle$ , $R = \langle R_1, R_2,, R_l \rangle$ , $fld$ , $new$ ) by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) <i>new</i> is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld$ , $new$ ) was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,P_k P_2,, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k), (NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Freees)$	$I_r$ was linearized f <i>LLX</i> results $(V_k, V_k),$ ALSE)})
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the valu des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( <b>return</b> $Help(des)$ > Freeze all Data-t	$V_k\rangle$ , $R = \langle R_1, R_2,, R_l \rangle$ , $fld$ , $new$ ) by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) <i>new</i> is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,P_k P_2,, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k), (NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Freerecords in des. V to protect their mutable fields from being change$	$I_r$ was linearized f <i>LLX</i> results $(V_k, V_k),$ ALSE)})
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew $(R_1, R_1), (R_2)$ (FLD, fld), ( <b>return</b> $Help(des)$ $\triangleright$ Freeze all Data-to $\langle nfreeze, nfinal, V_1 \rangle$	$V_k\rangle$ , $R = \langle R_1, R_2,, R_l \rangle$ , $fld$ , $new$ ) by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) $new$ is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),, V_k, R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k), (NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Factorrecords in des. V to protect their mutable fields from being changeV_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,$	$I_r$ was linearized f <i>LLX</i> results $(V_k, V_k),$ ALSE)})
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew $(R_1, R_1), (R_2)$ (FLD, fld), return $Help(des)$ > Freeze all Data-to $\langle nfreeze, nfinal, V_1$ for $i = 1nfreez$	$V_k\rangle$ , $R = \langle R_1, R_2,, R_l \rangle$ , $fld$ , $new$ ) by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) $new$ is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),, V_k, R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k), (NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Factorrecords in des. V to protect their mutable fields from being changeV_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new, e do$	$I_r$ was linearized f <i>LLX</i> results $(V_k, V_k),$ ALSE)}) d by other <i>SCX</i> s old := <i>ReadImmutables</i> ( <i>SCXdes</i> , <i>des</i> )
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew $(R_1, R_1), (R_2)$ (FLD, fld), ( <b>return</b> $Help(des)$ > Freeze all Data-1 $\langle nfreeze, nfinal, V_1$ <b>for</b> $i = 1nfreez$ <b>if not</b> CAS	$V_k\rangle$ , $R = \langle R_1, R_2,, R_l \rangle$ , $fld$ , $new$ ) by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) $new$ is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Factores_k)records in des. V to protect their mutable fields from being change(V_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,e do(V_i.info, des_i, des) then$	$I_r$ was linearized f <i>LLX</i> results $(V_k, V_k),$ ALSE)})
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( <b>return</b> $Help(des)$ > Freeze all Data-1 $\langle nfreeze, nfinal, V_1$ <b>for</b> $i = 1nfreez$ <b>if not</b> CAS <b>if</b> $V_i.info = 1$	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),, V_n, R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k), (NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, FactorV_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new, e do(V_i.info, des_i, des) then\neq des then$	$I_r$ was linearized f <i>LLX</i> results $(V_k, V_k),$ ALSE)}) d by other <i>SCX</i> s old := <i>ReadImmutables</i> ( <i>SCXdes</i> , <i>des</i> )
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew $(R_1, R_1), (R_2)$ (FLD, fld), return $Help(des)$ > Freeze all Data- $\langle nfreeze, nfinal, V_1$ for $i = 1nfreez$ if not CAS if $V_i.info = 0$ > Could r	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table o the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),, V_n, R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k), (NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, FAes)records in des. V to protect their mutable fields from being change(V_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new, ee do(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCX$	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data- (nfreeze, nfinal, V <sub>1</sub> for $i = 1nfreez$ if not CAS if $V_i.info =$ > Could r if Read	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table o te for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Factor(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCX[Field(SCXdes, des, ALLFROZEN) = TRUE then$	$I_r$ was linearized f <i>LLX</i> results $(V_k, V_k),$ ALSE)}) d by other <i>SCX</i> s old := <i>ReadImmutables</i> ( <i>SCXdes</i> , <i>des</i> )
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data- (nfreeze, nfinal, V <sub>1</sub> for $i = 1nfreez$ if not CAS if $V_i.info =$ > Could r if Read > the S	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table o te for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Factore^{cords} in des. V to protect their mutable fields from being change(V_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,e^{c} do(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCXHield(SCXdes, des, ALLFROZEN) = TRUE thenSCX$ has already completed successfully	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data-t $\langle nfreeze, nfinal, V_1$ for $i = 1nfreeze$ if not CAS if $V_i.info =$ > Could r if Read > the S return	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table o te for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Factor(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCX[Field(SCXdes, des, ALLFROZEN) = TRUE then$	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return Help(des) > Freeze all Data-t $\langle nfreeze, nfinal, V_1$ for $i = 1nfreeze$ if not CAS if $V_i.info =$ > Could r if Read > the S return else	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),, R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k), (NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Filter, Science, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new, e do(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCXWield(SCXdes, des, ALLFROZEN) = TRUE$ <b>then</b> SCX has already completed successfully <b>rn</b> TRUE	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data-t $\langle nfreeze, nfinal, V_1$ for $i = 1nfreeze$ if not CAS if $V_i.info =$ > Could r if Read > the S return else > Ator	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Filter,V_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,e do(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCXWield(SCXdes, des, ALLFROZEN) = TRUE$ then SCX has already completed successfully rn TRUE nically unfreeze all Data-records frozen for this $SCX$	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$ $ALSE) \})$ $d \text{ by other } SCXs$ $old \rangle := ReadImmutables(SCXdes, des)$ $\triangleright \text{ freezing CAS}$ $\triangleright \text{ frozen check step}$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data-t $\langle nfreeze, nfinal, V_1$ for $i = 1nfreeze$ if not CAS if $V_i.info =$ > Could r if Read > the S return else > Ator	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),, R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k), (NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Filter, Science, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new, e do(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCXWield(SCXdes, des, ALLFROZEN) = TRUE$ <b>then</b> SCX has already completed successfully <b>rn</b> TRUE	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data $\langle nfreeze, nfinal, V_1$ for $i = 1nfreeze$ if not CAS if $V_i.info = 1$ > Could r if Read > the S return else > Atom Writel	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Filter,V_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,e do(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCXWield(SCXdes, des, ALLFROZEN) = TRUE$ then SCX has already completed successfully rn TRUE nically unfreeze all Data-records frozen for this $SCX$	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$ $ALSE) \})$ $d \text{ by other } SCXs$ $old \rangle := ReadImmutables(SCXdes, des)$ $\triangleright \text{ freezing CAS}$ $\triangleright \text{ frozen check step}$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), return $Help(des)$ > Freeze all Data- (nfreeze, nfinal, V <sub>1</sub> for $i = 1nfreez$ if not CAS if $V_i.info =$ > Could r if Read > the S return else > Ator Writel return	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table o te for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, FAes)records in des. V to protect their mutable fields from being change(V_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,e$ do $(V_i.info, des_i, des)$ then $\neq des$ then not freeze $V_i$ because it is frozen for another $SCX$ IField(SCXdes, des, ALLFROZEN) = TRUE then SCX has already completed successfully rn TRUE mically unfreeze all Data-records frozen for this $SCX$ Field(SCXdes, des, STATE, Aborted) rn FALSE	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$ $ALSE) \})$ $d \text{ by other } SCXs$ $old \rangle := ReadImmutables(SCXdes, des)$ $\triangleright \text{ freezing CAS}$ $\triangleright \text{ frozen check step}$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data- (nfreeze, nfinal, V <sub>1</sub> for $i = 1nfreez$ if not CAS if $V_i.info =$ > Could r if Read > the S return else > Atom Writeh return	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table o re for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, FArecords in des. V to protect their mutable fields from being changeV_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,e$ do $(V_i.info, des_i, des)$ then $\neq des$ then not freeze $V_i$ because it is frozen for another $SCX$ Field(SCXdes, des, ALLFROZEN) = TRUE then SCX has already completed successfully rn TRUE mically unfreeze all Data-records frozen for this $SCX$ Field(SCXdes, des, STATE, Aborted) rn FALSE g Data-records (Assert: $state \in \{InProgress, Committed\})$	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data- (nfreeze, nfinal, V <sub>1</sub> for $i = 1nfreez$ if not CAS if $V_i.info =$ > Could r if Read > the S return else > Atom WriteField(SCXdefield)	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table o re for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, FArecords in des. V to protect their mutable fields from being changeV_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,e$ do $(V_i.info, des_i, des)$ then $\neq des$ then not freeze $V_i$ because it is frozen for another $SCX$ Wield(SCXdes, des, ALLFROZEN) = TRUE then SCX has already completed successfully rn TRUE mically unfreeze all Data-records frozen for this $SCX$ Wield(SCXdes, des, STATE, Aborted) rn FALSE g Data-records (Assert: $state \in \{InProgress, Committed\})$ (s, des, ALLFROZEN, TRUE)	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$ $ALSE) \})$ $d \text{ by other } SCXs$ $old \rangle := ReadImmutables(SCXdes, des)$ $\triangleright \text{ freezing CAS}$ $\triangleright \text{ frozen check step}$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data- (nfreeze, nfinal, V <sub>1</sub> for $i = 1nfreez$ if not CAS if $V_i.info =$ > Could r if Read > the S return else > Ator WriteField(SCXdef for $i = 1nfinal$	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results ( $SCXdes$ , {(NFREEZE, $k$ ), (NFINALIZE, $l$ ), ( $V_1, V_1$ ), ( $V_2, V_2$ ),, $v_rR_2$ ),, ( $R_l, R_l$ ), (DES <sub>1</sub> , $des_1$ ), (DES <sub>2</sub> , $des_2$ ),, (DES <sub>k</sub> , $des_k$ ), (NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, FA 255) records in $des$ . V to protect their mutable fields from being change $v_rV_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,$ e do ( $V_i.info, des_i, des$ ) then $\neq des$ then not freeze $V_i$ because it is frozen for another $SCX$ Wield(SCXdes, des, ALLFROZEN) = TRUE then SCX has already completed successfully rn TRUE mically unfreeze all Data-records frozen for this $SCX$ Field(SCXdes, des, STATE, Aborted) rn FALSE g Data-records (Assert: $state \in \{$ InProgress, Committed $\}$ ) s, des, ALLFROZEN, TRUE) do	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$ $ALSE)})$ $d \text{ by other } SCXs$ $old \rangle := ReadImmutables(SCXdes, des)$ $\triangleright \text{ freezing CAS}$ $\triangleright \text{ frozen check step}$ $\triangleright \text{ abort step}$ $\triangleright \text{ frozen step}$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data- (nfreeze, nfinal, V <sub>1</sub> for $i = 1nfreez$ if not CAS if $V_i.info =$ > Could r if Read > the S return else > Ator WriteField(SCXdef for $i = 1nfinal$ $R_i.marked := 7$	$V_k\rangle, R = \langle R_1, R_2,, R_l\rangle, fld, new \rangle$ by process $p$ for each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before desk be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results $(SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,R_2),, (R_l, R_l), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, FAess)records in des. V to protect their mutable fields from being change(V_i.info, des_i, des) then\neq do(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCXUField(SCXdes, des, ALLFROZEN) = TRUE$ then SCX has already completed successfully rn TRUE mically unfreeze all Data-records frozen for this $SCX$ Field(SCXdes, des, STATE, Aborted) rn FALSE g Data-records (Assert: $state \in \{InProgress, Committed\})$ s, des, ALLFROZEN, TRUE) do TRUE	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$ $ALSE)})$ $d \text{ by other } SCXs$ $old \rangle := ReadImmutables(SCXdes, des)$ $\triangleright \text{ freezing CAS}$ $\triangleright \text{ frozen check step}$ $\triangleright \text{ abort step}$ $\triangleright \text{ frozen step}$ $\triangleright \text{ mark step}$
> Preconditions: (1) f Let $des_1, des_2,,$ Let $old$ be the value des := CreateNew (R <sub>1</sub> , R <sub>1</sub> ), (R <sub>2</sub> (FLD, fld), ( return $Help(des)$ > Freeze all Data- (nfreeze, nfinal, V <sub>1</sub> for $i = 1nfreez$ if not CAS if $V_i.info =$ > Could r if Read > the S return else > Atom WriteField(SCXdef for $i = 1nfinal$ $R_i.marked := T$ CAS(fld, old, new	$V_k \rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle \text{ by process } p$ or each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results ( $SCXdes$ , {(NFREEZE, $k$ ), (NFINALIZE, $l$ ), ( $V_1, V_1$ ), ( $V_2, V_2$ ),, $r_R_2$ ),, ( $R_l, R_l$ ), (DES <sub>1</sub> , $des_1$ ), (DES <sub>2</sub> , $des_2$ ),, (DES <sub>k</sub> , $des_k$ ), (NEW, new), (OLD, $old$ ), (STATE, InProgress), (ALLFROZEN, $F_{2s}$ ) records in $des$ . V to protect their mutable fields from being change $V_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,$ e do ( $V_i.info, des_i, des$ ) then $\neq des$ then not freeze $V_i$ because it is frozen for another $SCX$ [Field( $SCXdes, des, ALLFROZEN$ ) = TRUE then SCX has already completed successfully rn TRUE mically unfreeze all Data-records frozen for this $SCX$ Field( $SCXdes, des, STATE$ , Aborted) rn FALSE g Data-records (Assert: $state \in \{$ InProgress, Committed $\}$ ) s, des, ALLFROZEN, TRUE) do FRUE $v_i$	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$ $ALSE)})$ $d \text{ by other } SCXs$ $old \rangle := ReadImmutables(SCXdes, des)$ $\triangleright \text{ freezing CAS}$ $\triangleright \text{ frozen check step}$ $\triangleright \text{ abort step}$ $\triangleright \text{ frozen step}$
<pre>&gt; Preconditions: (1) f Let <math>des_1, des_2,,</math> Let <math>old</math> be the value des := CreateNew (R<sub>1</sub>, R<sub>1</sub>), (R<sub>2</sub> (FLD, fld), ( return Help(des) &gt; Freeze all Data-t (nfreeze, nfinal, V<sub>1</sub> for <math>i = 1nfreeze</math> if not CAS if <math>V_i.info =</math> &gt; Could r if Read &gt; the S return else &gt; Atom WriteField(SCXdef for <math>i = 1nfinal</math> R<sub>i</sub>.marked := T CAS(fld, old, new &gt; Finalize all R<sub>i</sub> im</pre>	$V_k\rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle$ by process $p$ or each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table o the for $fld$ stored in $p$ 's local table of $LLX$ results ( $SCXdes, \{(NFREEZE, k), (NFINALIZE, l), (V_1, V_1), (V_2, V_2),,, R_2),, (R_1, R_1), (DES_1, des_1), (DES_2, des_2),, (DES_k, des_k),(NEW, new), (OLD, old), (STATE, InProgress), (ALLFROZEN, Fries)records in des. V to protect their mutable fields from being changeV_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new, edo(V_i.info, des_i, des) then\neq des thennot freeze V_i because it is frozen for another SCX[Field(SCXdes, des, ALLFROZEN) = TRUE thenSCX$ has already completed successfully <b>rn</b> TRUE mically unfreeze all Data-records frozen for this $SCX$ Field( $SCXdes, des, STATE, Aborted$ ) <b>rn</b> FALSE g Data-records (Assert: $state \in \{InProgress, Committed\}$ ) ( $s, des, ALLFROZEN, TRUE$ ) <b>do</b> (FRUE v) $R$ , and unfreeze all $V_i$ in $V$ that are not in $R$	<pre># Ir was linearized f LLX results (Vk,Vk), ALSE)})  d by other SCXs old &gt; := ReadImmutables(SCXdes, des)</pre>
<pre>&gt; Preconditions: (1) f Let <math>des_1, des_2,,</math> Let <math>old</math> be the value des := CreateNew (R<sub>1</sub>, R<sub>1</sub>), (R<sub>2</sub> (FLD, fld), ( return Help(des) &gt; Freeze all Data-t (nfreeze, nfinal, V<sub>1</sub> for <math>i = 1nfreeze</math> if not CAS if <math>V_i.info =</math> &gt; Could r if Read &gt; the S return else &gt; Atom WriteField(SCXdef for <math>i = 1nfinal</math> R<sub>i</sub>.marked := T CAS(fld, old, new &gt; Finalize all R<sub>i</sub> im</pre>	$V_k \rangle, R = \langle R_1, R_2,, R_l \rangle, fld, new \rangle \text{ by process } p$ or each $r$ in $V$ , $p$ has performed an invocation $I_r$ of $LLX(r)$ linked (2) new is not the initial value of $fld$ (3) for each $r$ in $V$ , no $SCX(V', R', fld, new)$ was linearized before $des_k$ be the descriptor pointers for $V_1, V_2,, V_k$ in $p$ 's local table of the for $fld$ stored in $p$ 's local table of $LLX$ results ( $SCXdes$ , {(NFREEZE, $k$ ), (NFINALIZE, $l$ ), ( $V_1, V_1$ ), ( $V_2, V_2$ ),, $r_R_2$ ),, ( $R_l, R_l$ ), (DES <sub>1</sub> , $des_1$ ), (DES <sub>2</sub> , $des_2$ ),, (DES <sub>k</sub> , $des_k$ ), (NEW, new), (OLD, $old$ ), (STATE, InProgress), (ALLFROZEN, $F_{2s}$ ) records in $des$ . V to protect their mutable fields from being change $V_2,, V_{nfreeze}, R_1, R_2,, R_{nfinal}, des_1, des_2,, des_{nfreeze}, fld, new,$ e do ( $V_i.info, des_i, des$ ) then $\neq des$ then not freeze $V_i$ because it is frozen for another $SCX$ [Field( $SCXdes, des, ALLFROZEN$ ) = TRUE then SCX has already completed successfully rn TRUE mically unfreeze all Data-records frozen for this $SCX$ Field( $SCXdes, des, STATE$ , Aborted) rn FALSE g Data-records (Assert: $state \in \{$ InProgress, Committed $\}$ ) s, des, ALLFROZEN, TRUE) do FRUE $v_i$	$I_r \text{ was linearized}$ $f LLX \text{ results}$ $(V_k, V_k),$ $ALSE) \})$ $d \text{ by other } SCXs$ $old \rangle := ReadImmutables(SCXdes, des)$ $\triangleright \text{ freezing CAS}$ $\triangleright \text{ frozen check step}$ $\triangleright \text{ abort step}$ $\triangleright \text{ frozen step}$ $\triangleright \text{ mark step}$

**Figure 5** Code for the *LLX* and *SCX* algorithm using the *mutable descriptor* ADT.

- P2. A marked Data-record remains marked forever.
- P3. A marked Data-record cannot point to an SCX-record with state = Aborted.
- P4. Each time the *des* field of a Data-record changes, it changes to a new value that has never previously been stored there (to avoid the ABA problem).

There is only one place in the code where an invocation I of ReadField(SCX-record, d, f, dv) can occur outside of Help(des): at line 4 of LLX in Figure 5. I reads the *state* field of d. We choose the default value dv = Committed for I. We give a rigorous, but straightforward, proof that this extended transformation of LLX and SCX is correct.

Let e be an execution of the original LLX and SCX algorithm  $\mathcal{A}$ , and let e' be an execution that is the same as e, except that one arbitrary SCX-record d becomes invalid at some point t after the SCX operation attempt O that created d terminates. Let O' be any LLX in e which, after t, performs an invocation I of *ReadField* on d outside of Help(d). We must prove that O' performs the exact same changes in e and e' to any variables that are still defined after O' terminates, and returns the same response in both executions.

Since I is invalid in e', by definition, the SCX O that created d must have terminated before I. Thus, by P1, I must return Committed or Aborted in e. If I returns Committed in e, then I returns the same response in e and e', so O' is exactly the same in both executions. Now, suppose I returns Aborted in e. We consider three cases, depending on where O' returns in e.

Case 1: O' returns at line 10 in e. If  $marked_2 = FALSE$ , then O' behaves exactly the same way in e and e'. So, suppose  $marked_2 = TRUE$ . Then, O' will enter the if-statement at line 6 in e, but not in e'. In this case, O' saw that the Data-record r pointed to an SCX-record with state = Aborted when it performed line 3, and that r was marked when it performed line 5. By P3, r cannot simultaneously be marked and point to an SCX-record with state = Aborted, so r.des must change between these two lines. By P4, it must change to a value different from rdes, so the if-block at line 8 will not be executed in e. However, this contradicts our assumption that O' returns at line 10.

Case 2: O' returns FINALIZED at line 12 in e. Observe that O' does not execute line 9 in e (since it would then return at the following line). We first prove that O' does not execute line 9 in e'. Since O' sees  $marked_1 = \text{TRUE}$  just before returning at line 12 in e, P2 implies that  $marked_2 = \text{TRUE}$  (in both e and e'). Since I returns Committed in e', O' will not enter the if-block at line 6 in e'. Thus, O' reaches line 11 in both e and e'.

Since I returns Committed in e', and we have assumed I returns Aborted in e, O' will not invoke Help at line 11 in e or e'. Therefore, O' does not change any variable that is still defined after it terminates. So, it suffices to prove that O' returns FINALIZED (at line 12) in e'. However, this is immediate from the fact that  $marked_1 = \text{TRUE}$  in O' in e (and, hence, in e').

Case 3: O' returns FAIL at line 13 in e. The proof is similar to the previous case, except  $marked_1 = FALSE$  in O' in e, so when O' reaches line 12, it will enter the *else*-block and return FAIL in both e and e'.

#### 5 Implementing the extended weak descriptor ADT

We give a brief high-level overview of our implementation. It uses largely known techniques (similar to [24]), and is not the main contribution of this work. Each process p uses a single descriptor object  $D_{T,p}$  in shared memory to represent all descriptors of type T that it ever creates. The descriptor object  $D_{T,p}$  conceptually represents p's current descriptor of type T. At different times in an execution,  $D_{T,p}$  represents different abstract descriptors created by p. We store a sequence number in  $D_{T,p}$  that is incremented every time p performs CreateNew(T, -). Instead of using traditional descriptor pointers, we represent each descriptor pointer as a pair of fields stored in a single word. These fields contain the name of the process who owns the descriptor, and a sequence number that indicates which invocation of CreateNew conceptually created this descriptor. When a descriptor pointer is passed to an operation O on the abstract descriptor, O compares the sequence number in des with the current sequence number in  $D_{T,p}$  to determine whether the operation is valid or invalid. Thus, incrementing the sequence number in  $D_{T,p}$  effectively makes all abstract descriptors of type T that were previously created by p invalid. Mutable fields are stored in a single word alongside a sequence number, so they can be updated with CAS, preventing invalid operations from making changes. (If the mutable fields and a sequence number to each word.)

#### 5.1 Detailed description

Complete pseudocode appears in Figure 6. We start by describing the data types and shared variables. Each descriptor contains zero or more immutable fields, and zero or more mutable fields (which are determined by the *descriptor type*), as well as a sequence number field seq. Recall that  $D_{T,p}$  represents different abstract descriptors at different times. Note that the immutable fields of  $D_{T,p}$  are only immutable for as long as  $D_{T,p}$  represents the same abstract descriptor. When  $D_{T,p}$  is reused, so that it represents a different abstract descriptor, its immutable fields can be reinitialized. Usually very few bits are required for the mutable fields, since they exist solely to capture the state of an ongoing operation (and it is inefficient to frequently change the state of a descriptor). (Every lock-free algorithm we are aware of uses at most a small constant number of bits for its mutable fields.) Consequently, we think of the sequence field and the mutable fields of a descriptor d as being packed together in a single word *mutables* of d (with subfields for the sequence field and each mutable field). (Note that, if more space is needed for mutable fields in some future algorithm, we can eliminate this assumption about the size of *mutables*, as we explain below.) We use d fto denote an immutable field f of d, d-mutables to denote the field mutables of d, and d.mutables.f to denote a mutable field f of d.

Since *mutables* fits in a single word, it can be modified atomically using CAS. By having CAS atomically operate on a mutable field and the sequence number, we can ensure that a descriptor changes only if its sequence number has not changed.

We now describe the operations. An invocation of CreateNew(T,...) by process p first increments the sequence number of  $D_{T,p}$ , then initializes all of its fields, then increments the sequence number again and returns a new descriptor pointer (with the up-to-date sequence number). Observe that the descriptor pointers returned by CreateNew always have even sequence numbers, and the sequence number of a descriptor is odd while it is being initialized by CreateNew. Consequently, while a descriptor is being initialized, its sequence number does not match any descriptor pointer in the system, so no process can read or modify the descriptor's fields.

Note that this approach of incrementing a sequence number twice has been used in different contexts such as in transactional memory, where the least significant bit represents whether the sequence number is locked or unlocked. Here, the idea is slightly different, since the least significant bit represents whether the descriptor is currently being reused and initialized, or is safe to access. (Nevertheless, in some sense, one can think of the bit indicating whether the descriptor is currently being initialized as a sort of lock. It does not prevent other processes from making progress (since operations on the descriptor will

```
> Data types
 1
     Descriptor of type T :
\mathbf{2}
        mutables = \langle seq, mut_1, mut_2, ... \rangle
                                                                                                           \triangleright Mutable fields
3
                                                                                                        \triangleright Immutable fields
        imm_1, imm_2, \dots
 4
     ▷ Shared variables
 6
        D_{T,p} for each descriptor type T and process p
 7
    \triangleright ADT operations
9
     CreateNew(T, v_1, v_2, ...) by process p:
10
11
        oldseq := D_{T,p}.mutables.seq
        D_{T,p}.mutables.seq := oldseq + 1
for each field f in D_{T,p}
12
^{13}
            let value be the corresponding value in \{v_1, v_2, ...\}
14
            if f is immutable then
15
              D_{T,p}.f := value
16
            else
17
               D_{T,p}.mutables.f := value
18
        D_{T,p}.mutables.seq := oldseq + 2
19
        return \langle p, oldseq + 2 \rangle
20
     ReadField(des, f, dv):
22
         \langle q, seq \rangle := des
^{23}
         if f is immutable then
^{24}
           result := D_{T,q} f
^{25}
26
        else
           result := D_{T,q}.mutables.f
27
28
         if seq \neq D_{T,q}.mutables.seq then return dv
        return result
29
     ReadImmutables(des):
31
        \langle q, seq \rangle := des
32
        for each f in des
33
            if f is immutable then add D_{T,q}. f to result
34
        if seq \neq D_{T,q}.mutables.seq then return \perp
35
        return result
36
      WriteField(des, f, value):
38
        \langle q, seq \rangle := des
39
40
        loop
           exp := D_{T,q}.mutables
41
            if exp.seq \neq seq then return
^{42}
           new := exp
43
           new.f := value
44
^{45}
            if CAS(\&D_{T,q}.mutables, exp, new) then return
47
     CASField(des, f, fexp, fnew):
        \langle q, seq \rangle := des
48
        loop
49
           exp := D_{T,q}.mutables
50
           if exp.seq \neq seq then return \perp
if exp.f \neq fexp then return exp.f
51
52
           new := exp
53
           new.f := fnew
54
            if CAS(\&D_{T,q}.mutables, exp, new) then
55
               return fnew
56
```

**Figure 6** Pseudocode for the *extended weak descriptor* ADT implementation.

terminate, but will simply be invalid), but it does prevent them from accessing fields of the descriptor as they are being changed.)

An invocation of ReadField(des, f, default) by p reads the value v of the mutable or immutable field f from  $D_{T,p}$  followed by its sequence number s. If s matches the sequence number in the descriptor pointer des, then v is returned. Otherwise, default is returned.

*ReadImmutables* is similar to *ReadField*, except it reads all immutable fields, instead of a single field, and it returns  $\perp$  instead of *default*.

An invocation I of WriteField(des, f, value) by p performs a sequence of one or more attempts. In each attempt, it reads the contents old of mutables, including the sequence number s, from  $D_{T,p}$ , then checks whether s matches the sequence number in the descriptor pointer des. If the sequence numbers do not match, then the abstract descriptor represented by des is invalid, so I returns without changing f. Otherwise, I uses CAS to try to change  $D_{T,p}$ .mutables from old to new, which is a copy of old in which the contents of field f have been changed (locally) to contain value. Observe that this CAS will succeed only if the sequence number in  $D_{T,p}$ .mutables matches the sequence number in des. If the CAS succeeds, then I returns. Otherwise, I performs another attempt.

Note that *WriteField* is less efficient than performing a direct write to memory. However, since mutable fields are used merely to encode the status of an ongoing operation, there are usually very few changes to a descriptor.

CASField is quite similar to WriteField. The only differences are (1) CASField has different return values and, (2) in each attempt, it performs an additional check to determine whether old.f is equal to fexp, and, if not, returns old.f.

#### 5.2 Practical considerations

One might wonder, in an algorithm with multiple types of descriptors, why the type of a descriptor is not also encoded in descriptor pointers. In algorithms that use multiple descriptor types, any time the original algorithm accesses a field of a descriptor, it typically must know what kind of descriptor it is accessing (if, for no other reason, to compute the address of the desired field within the descriptor). In such algorithms, it would not be necessary for descriptor pointers to carry this extra information. For algorithms that access descriptors without knowing their exact types, one can include the descriptor type in descriptor pointers.

Some lock-free algorithms "steal" up to three bits from pointers to encode additional information, typically to distinguish between application values and (potentially, various types of) descriptors. To accommodate such algorithms, one can slightly shrink the sequence number in our descriptor pointers, and reserve the three lowest-order bits for use by other algorithms.

One obvious way to store the descriptors for each thread is to create an array for each descriptor type, with a slot containing a descriptor for each process. In this kind of implementation, it is extremely important to pad each slot to avoid false sharing [5]. We suggest allocating at least two cache lines for each descriptor (128 bytes on modern Intel and AMD machines).

To improve efficiency, modern Intel and AMD processors implement a relaxed memory model called total store order (TSO) that allows certain steps in a program to be executed out of order. Specifically, a read that occurs after a write in a program can actually be executed *before* the write, as long as the read and write are not accessing the same address. This can render a concurrent algorithm incorrect if it requires a write by a process p to be visible to other processes *before* p performs a subsequent read. One can prevent this reordering by

placing a memory fence (or barrier) between the write and read. CAS instructions also act as memory fences. Our implementation does not require any memory fences (beyond those implied by CAS instructions). This is an attractive property, since memory fences incur high overhead.

Our implementation uses unbounded sequence numbers. However, in practice, sequence numbers are bounded, and they may wrap around. If wraparound occurs, then two invocations of *CreateNew* might return the same descriptor pointer. This can cause an *ABA* problem if the high-level algorithm that uses descriptors relies on the uniqueness of descriptor pointers returned by *CreateNew*.

We argue that the sequence number can be made sufficiently large on modern systems for this to be a non-issue. Consider a system with a 64-bit word size. Recall that a sequence number appears both in each descriptor pointer, and also in the *mutables* field of each descriptor. A descriptor pointer contains only a process name and a sequence number, so if n bits are reserved for the process name, then 64 - n bits remain for the sequence number. The *mutables* field contains the descriptor's mutable fields and a sequence number, so if m bits are reserved for mutable fields, then 64 - m bits remain for the sequence number. Thus, if we use 14-bit process names (as the Linux kernel does), and the mutable fields of each descriptor fit in at most 14 bits, then 50 bits remain for the sequence number. We are unaware of any algorithm that requires more than three bits for mutable fields in its descriptors, so this is realistic. In this case, a single process must perform  $2^{50}$  operations to trigger even a single wraparound. If we assume that a single process can perform one million operations per second, this will take 35 years of continuous execution. If this is still a concern, then one can use double-wide CAS (DWCAS), which is implemented on modern Intel and AMD systems, instead of CAS, to atomically operate on two adjacent words (containing a much larger sequence number).

Although we are unaware of any current lock-free algorithms that use more than three bits for mutable fields in descriptors, some future algorithm may use more. If the mutable fields of a descriptor cannot fit in the same word as a sequence number, then our approach must be modified. If the mutable fields and a sequence number can fit in two adjacent words, then one can simply use DWCAS instead of CAS. Otherwise, one can store mutable fields in their own separate words, and *replicate* the sequence number, storing a copy in the word adjacent to each mutable field. To change a mutable field, one would then perform DWCAS on the word containing the mutable field, and its adjacent sequence number. When the descriptor is reused, instead of incrementing a single sequence number, one would increment all sequence numbers.

In order to choose how many bits should be devoted to the process name in descriptor pointers, one must know an upper bound on the number of processes. We stress that this is not an onerous constraint, because the upper bound does not need to be tight. Note that one need not initially allocate descriptors for all processes that *could* be running in the system. It is straightforward to allocate a descriptor for a process the first time it invokes *CreateNew* (potentially even in batches, to amortize the cost and improve control over memory layout).

#### 5.3 Correctness

We now prove that our implementation is linearizable. We first give the linearization points for all operations.

- Each invocation of *CreateNew* is linearized at the increment of the sequence number at line 12.
- If an invocation I of ReadField(des, f, dv) returns at line 28, then it is linearized at the read of the sequence number at the same line. If I returns at line 29, then it is linearized at the preceding read of the field f: for immutable fields this is line 25, and for mutable fields this is line 27.
- Each invocation of *ReadImmutables* is linearized at the read of the sequence number at line 35.
- If an invocation I of WriteField(des, f, value) returns at line 42, then it is linearized at the last read of the sequence number at the same line. If I returns at line 45, then it is linearized at the successful CAS at the same line.
- If an invocation I of CASField(des, f, fexp, fnew) returns at line 51, then it is linearized at the last read of the sequence number at the same line. If I returns at line 56, then it is linearized at the successful CAS at the previous line. If I returns at line 52, then it is linearized at the last read at the same line.

▶ Observation 1. The sequence number of  $D_{T,p}$  (also denoted  $D_{T,p}$ .mutables.seq) is written only by p in invocations of CreateNew(T, -).

▶ Observation 2. Every descriptor pointer returned by CreateNew has an even sequence number, and the linearization point of CreateNew always changes the sequence number of the descriptor to an odd number.

▶ Observation 3. The sequence number returned by a

CreateNew(T, -) operation by p is 2 + v where v is the sequence number returned by p's previous CreateNew(T, -) operation, or v = 0 if p has not performed CreateNew(T, -).

We now prove that the above linearization points are correct. Let e be an execution of our implementation of extended weak descriptors. Let  $O_1, O_2 \cdots O_k$  be the extended weak descriptor operations executed in e in the order they are linearized. Note that we prove correctness assuming unbounded sequence numbers. The implications of bounded sequence numbers were considered above.

▶ **Theorem 2.** The responses of  $O_1, O_2 \cdots O_k$  respect the semantics of the extended weak descriptor ADT.

**Proof.** By strong induction on the sequence of extended weak descriptor operations that terminate in e. Base case: the claim vacuously holds when no operations have returned. Induction step: assume the return values of  $O_1, O_2 \cdots O_{i-1}$  follow the semantics of the extended weak descriptor ADT. Let p be the process that performs  $O_i$ , and T be the type of descriptor on which  $O_i$  is performed.

Suppose  $O_i$  is a CreateNew(T, -) operation. By Observation 3,  $O_i$  returns a unique descriptor pointer.

In each of the following cases,  $O_i$  takes a descriptor pointer des as one of its arguments. Let q and seq be the process name sequence number in des, respectively. Let  $O_{init}$  be the CreateNew(T, -) by q that returned des. Since des is returned by  $O_{init}$  before it is passed to any operation,  $O_{init}$  is linearized before  $O_i$ .

XX:23

Suppose  $O_i$  is a *ReadField* that returns the default value at line 28, a *CASField* that returns  $\perp$  at line 51 or a *ReadImmutables* that returns  $\perp$  at line 35. We argue that *des* is invalid when  $O_i$  is linearized. In each case,  $O_i$  returns after seeing that the sequence number of  $D_{T,q}$  no longer contains *seq*. Thus, this sequence number must change after *des* is returned by  $O_{init}$ , and before  $O_i$  is linearized. By Observation 1, this change to the sequence number of  $D_{T,q}$  must be performed by a *CreateNew*(T, -) operation  $O_{change}$  by q (which occurs after  $O_{init}$ , and before  $O_i$  is linearized).  $O_{change}$  changes the sequence number twice, and is linearized at the first change. Thus,  $O_{change}$  is linearized after  $O_{init}$  and before  $O_i$  is linearized.

Now suppose  $O_i$  is a *ReadField* that returns at line 29, a *CASField* that returns at line 56, or a *ReadImmutables* that returns at line 36. We first argue that *des* is valid when  $O_i$  is linearized. In each case,  $O_i$  sees that the sequence number of  $D_{T,q}$  is *seq* at some time t, which is either when  $O_i$  is linearized, or is after  $O_i$  is linearized. By Observation 1 and Observation 3, whenever the sequence number of  $D_{T,q}$  is changed, it is changed to a new value that it never previously contained. Thus, since the sequence number of  $D_{T,q}$  contains *seq* when  $O_{init}$  terminates, and it contains *seq* at time t, it contains *seq* at all times after  $O_{init}$  terminates and before t. Hence, the sequence number of  $D_{T,q}$  contains *seq* when  $O_i$ is linearized. By Observation 1, q does not perform any *CreateNew*(T, -) after  $O_{init}$  and before t, so *des* is *valid* when  $O_i$  is linearized.

We now argue that the response of  $O_i$  is correct if it is a ReadField(des, f, dv). The proof is similar when  $O_i$  is a CASField or ReadImmutables.

If f is immutable, then it is changed only by CreateNew(T, -) operations by q. Since des is valid when  $O_i$  is linearized,  $O_{init}$  performs the last change to f before  $O_i$  is linearized. Recall that  $O_i$  start after  $O_{init}$  terminates. Thus, the write of f in  $O_{init}$  happens before the invocation of  $O_i$ , and  $O_i$  will return the value written to f by  $O_{init}$ .

If f is mutable, then let  $O_{change}$  be the operation that performs the last change to f before  $O_i$  is linearized, and v be the value that it stores in f. Observe that  $O_i$  returns v. We show that  $O_{change}$  is the last operation that changes f and is linearized before  $O_i$ . If  $O_{change}$  is the same as  $O_{init}$ , then we are done. Otherwise, since we have argued that q does not perform any CreateNew(T, -) after  $O_{init}$  and before t,  $O_{change}$  must be a WriteField or CASField. In each case,  $O_{change}$  can change f only once, with a successful CAS (at line 55 or line 45). Since  $O_{change}$  is linearized at this CAS, it is linearized before  $O_i$ . Moreover, since we have assumed that  $O_{change}$  is the last operation to change f before  $O_i$ , no other operation that changes f linearized after  $O_{change}$  and before  $O_i$ .

#### 5.4 Progress

Suppose, to obtain a contradiction, that there is an execution in which processes take infinitely many steps, but only finitely many (extended weak descriptor) operations terminate. Then, after some time t, no operation terminates, which means there is at least one operation O in which a process takes infinitely many steps. By inspection of Figure 6, O must be a WriteField or CASField operation. Suppose O is a WriteField operation. Then, each time O executes line 42, it sees old.seq = seq, and each time it executes line 45, its CAS fails and returns old without changing  $D_{T,q}$ .mutables. Observe that the CAS will fail only if  $D_{T,q}$ .mutables changes after it is read at line 41 and before the CAS at line 45. Thus,  $D_{T,q}$ .mutables changes infinitely many times in the execution. Since  $D_{T,q}$ .mutables can be changed only by WriteField or CASField operations, and any operation that changes  $D_{T,q}$ .mutables terminates, there must be infinitely many terminating WriteField or CAS-Field operations, which is a contradiction. The proof is similar when O is a CASField.

#### 6 Experiments

Our experiments were run on two large-scale systems. The first is a 2-socket Intel E7-4830 v3 with 12 cores per socket and 2 hyperthreads (HTs) per core, for a total of 48 threads. Each core has a private 32KB L1 cache and 256KB L2 cache (which is shared between HTs on a core). All cores on a socket share a 30MB L3 cache. The second is a 4-socket AMD Opteron 6380 with 8 cores per socket and 2 HTs per core, for a total of 64 threads. Each core has a private 16KB L1 data cache and 2MB L2 cache (which is shared between HTs on a core). All cores on a socket share a 6MB L3 cache.

Since both machines have multiple sockets and a non-uniform memory architecture (NUMA), in all of our experiments, we pinned threads to cores so that the first socket is filled first, then the second socket is filled, and so on. Furthermore, within each socket, each core has one thread pinned to it before hyperthreading is engaged. Consequently, our graphs clearly show the effects of hyperthreading and NUMA.

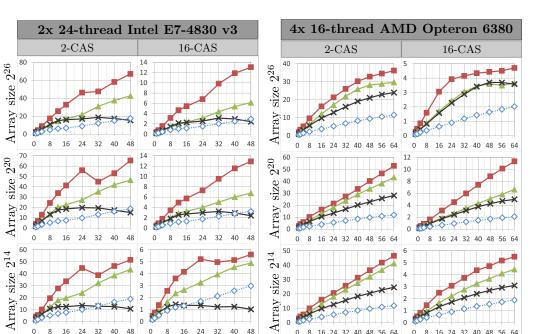
For example, on the Intel machine, from thread counts 1 to 12 all threads are running on a single socket and at most one thread is pinned to each core. (socket 1: no HTs; socket 2: empty). From 13 to 24, all threads are running on a single socket and cores either have one or two threads pinned to them (socket 1: HTs; socket 2: empty). From 25 to 36, each core on the first socket has two threads pinned to it, and the remaining threads are each pinned to unique cores on the second socket (socket 1: HTs; socket 2: no HTs). Finally, from 37 to 48, each core on the first socket has two threads pinned to threads pinned to it, and cores on the second socket have one or two threads pinned to them (socket 1: HTs; socket 2: no HTs).

Both machines have 128GB of RAM. Each runs Ubuntu 14.04 LTS. All code was compiled with the GNU C++ compiler (G++) 4.8.4 with build target  $x86_64$ -linux-gnu and compilation options -std=c++0x -mcx16 -03. Thread support was provided by the POSIX Threads library. We used the Performance Application Programming Interface (PAPI) library [12] to collect statistics from hardware performance counters to determine cache miss rates, stall times, instructions retired, and so on.

The system (glibc) allocator was found to have poor scaling and overall performance. Instead, we used jemalloc 4.2.1, a fast user-space allocator designed to minimize contention and improve scalability [15]. The library was dynamically linked with LD\_PRELOAD, which is the recommended method. This allocator was found to yield vastly superior performance for all algorithms, in all benchmarks. We also tried the tomalloc allocator from Google's Perftools library, which is another common choice for concurrency-friendly allocation. However, performance with tomalloc was substantially worse for all algorithms than with jemalloc.

On the AMD machine, transparent huge-pages were disabled manually in the jemalloc implementation by changing the default allocation chunk size from  $2^{21}$  to  $2^{19}$  using the environment parameter setting MALLOC\_CONF=1g\_chunk:19. This maintained or improved the performance for all algorithms in all workloads, and did not change the performance relationship between any pair of algorithms. The same change did not improve performance on the Intel machine (for any algorithm or workload), so the original chunk size was used.

For read-heavy workloads, it was necessary to force distribution of pages across NUMA nodes to get consistently high performance. To achieve this, we used numactl -interleave=all for all workloads. (Doing this did not negatively impact the performance of any workload, but its benefit was less noticeable for write-heavy workloads.)



48 🖶 Reuse 🛧 DEBRA Ӿ HP 🚸 RCU

**Figure 7** Results for a *k*-CAS microbenchmark. The x-axis represents the number of concurrent threads. The y-axis represents operations per microsecond.

0 8 16 24 32 40 48 56 64

0 8 16 24

32 40 48

#### 6.1 k-CAS microbenchmark

0

8 16 24 32 40

0

0

16 24 32 40 48 0

In order to compare our reusable descriptor technique with algorithms that reclaim descriptors, we implemented k-CAS with several memory reclamation schemes. Specifically, we implemented a lock-free memory reclamation scheme that aggressively frees memory called *hazard pointers* [26], a (blocking) epoch-based reclamation scheme called *DEBRA* [7], and reclamation using the read-copy-update (RCU) primitives [13] (also blocking). We use *Reuse* as shorthand for our reusable descriptor based algorithm, and DEBRA, HP and RCU to denote the other algorithms.

The paper by Harris et al. also describes an optimization to reduce the number of DCSS descriptors that are allocated by embedding them in the k-CAS descriptor. We applied this optimization, and found that it did not significantly improve performance. Furthermore, it complicated reclamation with hazard pointers. Thus, we did not use this optimization.

Methodology. We compared our implementations of k-CAS using a simple array-based microbenchmark. For each algorithm  $A \in \{Reuse, DEBRA, HP, RCU\}$ , array size  $S \in$  $\{2^{14}, 2^{20}, 2^{26}\}$  and k-CAS parameter  $k \in \{2, 16\}$ , we run ten timed *trials* for several thread counts n. In each trial, an array of a fixed size S is allocated and each entry is initialized to zero. Then, n concurrent threads run for one second, during which each thread repeatedly chooses k uniformly random locations in the array, reads those locations, and then performs a k-CAS (using algorithm A) to increment each location by one.

As a way of validating correctness in each trial, each thread keeps track of how many successful k-CAS operations it performs. At the end of the trial, the sum of entries in the array must be k times the total number of successful k-CAS operations over all threads.

**Results.** The results for this benchmark appear in Figure 7. Error bars are not drawn on the graphs, since more than 97% of the data points have a standard deviation that is less than 5% of the mean (making them essentially too small to see).

Overall, *Reuse* outperforms every other algorithm, in every workload, on both machines. Notably, on the Intel machine, its throughput is 2.2 times that of the next best algorithm at 48 threads with k = 16 and array size  $2^{26}$ . On the AMD machine, its throughput is 1.7 times that of the next best algorithm at 64 threads with k = 16 and array size  $2^{20}$ .

On the Intel machine, with k = 2, NUMA effects are quite noticeable for *Reuse* in the jump from 24 to 32 threads, as threads begin running on the second socket. According the statistics we collected with PAPI, this decrease in performance corresponds to an increase in cache misses. For example, with k = 2 and an array of size  $2^{26}$  in the Intel machine, jumping from 24 threads to 25 increases the number of L3 cache misses per operation from 0.7 to 1.6 (with similar increases in L1 and L2 cache misses and pipeline stalls). We believe this is due to cross-socket cache invalidations.

From the three graphs for k = 2 on Intel, we can see that the effect is more severe with larger absolute throughput (since the additive overhead of a cache miss is more significant). Conversely, the effect is masked by the much smaller throughput of the slower algorithms, and by the substantially lower throughputs in the k = 16 case, except when the array is of size  $2^{14}$ . In the array of size  $2^{14}$ , contention is extremely high, since each of the 48 threads are accessing 16 k-CAS addresses, each of which causes contention on the entire cache line of 8 words, for a total of 6144 array entries contended at any given time. Thus, cache misses become a dominating factor in the performance on two sockets. These effects were not observed on the AMD machine. There, the number of cache misses is not significantly different when crossing socket boundaries, which suggests a robustness to NUMA effects that is not seen on the Intel machine.

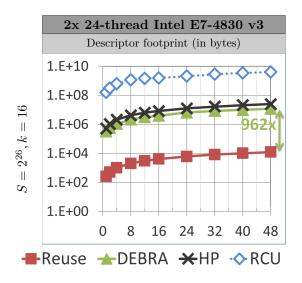
Interestingly, absolute throughputs on the AMD machine are larger with array size  $2^{20}$  than with sizes  $2^{14}$  and  $2^{26}$ . This is because the  $2^{20}$  array size represents a sweet spot with less contention than the  $2^{14}$  size and better cache utilization than the  $2^{26}$  size. For example, with 64 threads and k = 16, *Reuse* incurred approximately 50% more cache misses with size  $2^{26}$  than with size  $2^{20}$ , and approximately 50% of operations helped one another with size  $2^{14}$ , whereas less than 1% of operations helped one another with size  $2^{20}$ .

Note, however, that this is not true on the Intel machine. There,  $2^{26}$  is almost always as fast as  $2^{20}$ , because of the very large shared L3 cache (which is 5x larger than on the AMD machine). This is reflected in the increased number of cycles where the processor is stalled (e.g., waiting for cache misses to be served) when moving from size  $2^{20}$  to  $2^{26}$ . On the Intel machine, stalled cycles increase by 85% per operation, whereas on the AMD machine they increase by a whopping 450% per operation.

#### 6.1.1 Memory usage in the k-CAS benchmark

We studied memory usage for all algorithms, in all workloads, on both systems, but we only show results for array size  $2^{26}$  and k = 16, because the other graphs are very similar. These results appear in Figure 8. In particular, we are interested in the descriptor footprint, i.e., the maximum amount of memory ever occupied by descriptors in an execution. Unfortunately, computing the descriptor footprint exactly would require excessive synchronization between threads. Thus, we approximate the descriptor footprint by computing the descriptor footprint for each thread, and then summing those individual footprints. (This is only an approximation, since different threads may hit their peak memory usage for descriptors at different times.) The graph in Figure 8 contains the results of this approximation.

These results were obtained as follows. Each thread used three private variables: *total*-*Free*, *totalMalloc* and *maxFootprint*. Each time a thread invoked **free**, it incremented



**Figure 8** Memory usage for the *k*-CAS microbenchmark. The x-axis represents the number of concurrent threads. *Note the logarithmic scale.* 

totalFree by the size of the descriptor being freed. Each time a thread invoked malloc, it incremented totalMalloc by the size of the descriptor being allocated, and then set  $maxFootprint = max\{maxFootprint, totalMalloc-totalFree\}$ . The per-thread maxFootprints are then summed to obtain the data points in the graph.

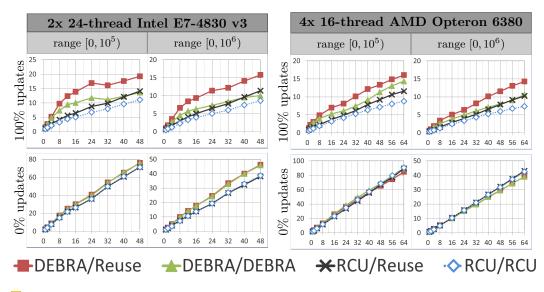
Note that the *y*-axis is a logarithmic scale. The results show that *DEBRA* and *HPs* use almost **three orders of magnitude** more memory than *Reuse* at their peaks, and *RCU* uses nearly three orders of magnitude more memory than *DEBRA* and *HPs*. *RCU*'s memory usage is significantly higher because reclamation is delayed significantly longer than in the other algorithms.

#### 6.2 BST microbenchmark

Unlike in the k-CAS algorithm, where memory reclamation was only needed for descriptors, in the BST, memory reclamation is always needed for nodes. To compare our technique with different memory reclamation options, we implemented four variants of the BST algorithm: DEBRA/DEBRA, DEBRA/Reuse, RCU/RCU and RCU/Reuse. Here, an algorithm named X/Y uses X to reclaim nodes and Y for descriptors. For example, DEBRA/Reuse uses DEBRA to reclaim nodes and has reusable descriptors.

Unfortunately, we could not create a variant of the BST using hazard pointers. As part of the *finalizing* mechanism, this BST implementation *marks* nodes before deleting them. Furthermore searches are allowed to traverse marked nodes, regardless of whether they have been deleted, and subsequently succeed. These algorithmic properties make it infeasible to use hazard pointers [7].

**Methodology.** We compared our BST variants using a simple randomized microbenchmark. For each algorithm  $A \in \{DEBRA/DEBRA, DEBRA/Reuse, RCU/RCU, RCU/Reuse\}$ , key range size  $K \in \{10^5, 10^6\}$  and update rate  $U \in \{100, 0\}$ , we run ten timed trials for several thread counts n. Each trial proceeds in two phases: prefilling and measuring. In the prefilling phase, n concurrent threads perform 50% Insert and 50% Delete operations on keys drawn uniformly randomly from [0, K) until the size of the tree converges to a steady state (containing approximately K/2 keys). Next, the trial enters the measuring phase,



**Figure 9** Results for a **BST microbenchmark**. The x-axis represents the number of concurrent threads. The y-axis represents operations per microsecond.

during which threads begin counting how many operations they perform. (These counts are eventually summed over all threads and reported in our graphs.) In this phase, each thread instead performs (U/2)% Insert, (U/2)% Delete and (100 - U)% Find operations on keys drawn uniformly from [0, K) for one second.

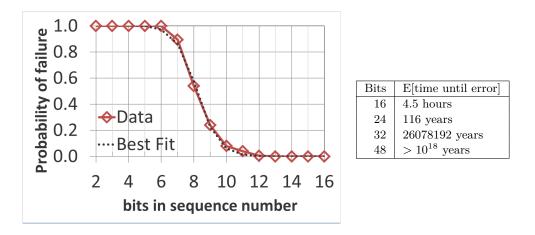
As a way of validating correctness in each trial, each thread maintains a *checksum*. Each time a thread inserts a new key, it adds the key to its checksum. Each time a thread deletes a key, it subtracts the key from its checksum. At the end of the trial, the sum of all thread checksums must be equal to the sum of keys in the tree.

**Results.** The results for this benchmark appear in Figure 9. The *Reuse* variants perform at least as well as the pure reclamation variants in every case, and significantly outperform the reclamation variants in the 100% update workload. Most notably, on the Intel machine with key range  $[0, 10^6]$  and 48 threads, DEBRA/Reuse outperforms DEBRA/DEBRA by 57%, and RCU/Reuse outperforms RCU/RCU by 33%. As expected, *Reuse* does not perform significantly faster than the reclamation variants in the workloads with no updates. This is because searches do not create descriptors. However, crucially, our transformation does not impose any overhead on searches, either.

#### 6.3 Studying sequence number wraparound

We performed experiments on the larger AMD machine to study how frequently errors occur when sequence numbers of varying bit-widths experience wraparound. For each bit-width  $B \in \{2, 3, 4, ..., 48\}$ , we performed 200 trials in which 64 threads run for 100 milliseconds before terminating. Each trial was the same as a trial in our BST experiments with 100% updates and key range  $[0, 10^5)$ .

We identified three different types of errors in these trials. First, at the end of a trial, the sum of the checksums maintained by all threads would fail to match the sum of keys in the tree. Second, threads would enter infinite loops due to the tree structure being corrupted, e.g., because a cycle was introduced. (We identified this type of error by waiting until some thread had run twice as long as it should have.) Third, an invalid memory access would



**Figure 10** Experiment studying sequence number wraparound.

cause immediate program failure (e.g., due to segmentation fault or bus error).

For each *B* value, we divided the number of failed runs by 200 to estimate the probability of a trial failing. A graph showing the resulting estimated probability distribution appears in Figure 10. For small *B* values, trials frequently experienced errors. However, for  $B \ge 13$ , we did not observe a single error in 200 trials (despite the fact that wraparound consistently occurred in every trial). For  $B \ge 16$ , trials were not sufficiently long for wraparound to consistently occur. The results appear in Figure 10.

As is common in physics when studying unknown functions, we make an educated guess that the distribution is sigmoidal, which means it is of the form  $f(x) = a/(1 + e^{-b(x-c)})$  for constants a, b and c. We determined a sigmoidal curve of best fit from the data, obtaining the function  $f(x) = 1/(1 + e^{1.53969(x-8.199181)})$ , which is plotted as the *Best Fit* curve on the graph in Figure 10. As the graph shows, the error between the best fit curve and the measured data is extremely small. Although we do not have a justification for the shape of this distribution, we think it is worthwhile to put forth a hypothesis and study its consequences.

We used f(x) to extrapolate on the data to estimate the expected time until an error occurs in this workload for several bit-widths that would be impractical to test experimentally. These extrapolations appear in the table on the right of Figure 10. They should be taken with a grain of salt, since the error in our estimation likely grows quickly with B. However, the extrapolations suggest that even B = 32 would be quite safe for this workload. To our knowledge, this kind of experimental exploration of the practicality of unbounded sequence numbers has not previously been done.

#### 7 Related Work

Several papers have presented universal constructions or strong primitives for non-blocking algorithms in which operations create descriptors [20, 2, 1, 27, 17, 23, 21, 24, 3, 11]. A subset of these algorithms employ ad-hoc techniques for reusing descriptors [20, 2, 1, 27, 24, 23, 21]. The rest assume descriptors will be allocated for each operation and eventually reclaimed.

Most of the ad-hoc techniques for reusing descriptors have significant downsides. Some are complex and tightly integrated into the underlying algorithm, or rely on highly specific algorithmic properties (e.g., that descriptors contain only a single word). Others use synchronization primitives that atomically operate on large words, which are not available on modern systems, and are inefficient when implemented in software. Yet others introduce high space overhead (e.g., by attaching a sequence number to *every* memory word). Some techniques also incur significant runtime overhead (e.g., by invoking expensive synchronization primitives just to *read fields* of a descriptor). Furthermore, these techniques give, at best, a vague idea of how one might reuse descriptors for arbitrary algorithms, and it would be difficult to determine how to use them in practice. Our work avoids all of these downsides, and provides a concrete approach for transforming a large class of algorithms.

Barnes [4] introduced a technique for producing non-blocking algorithms that can be more efficient (and sometimes simpler) than the universal constructions described above. With Barnes' technique, each operation creates a new descriptor. Creating a new descriptor for each operation allows his technique to avoid the ABA problem while remaining conceptually simple. Each operation conceptually locks each location it will modify by installing a pointer to its descriptor, and then performs it modifications and unlocks each location. Barnes' technique is the inspiration for the class WCA. Many algorithms have since been introduced using variants of this technique [17, 14, 3, 19, 29, 11, 10]. Several of these algorithms are quite efficient in practice despite the overhead of creating and reclaiming descriptors. Our technique can significantly improve the space and time overhead of such algorithms.

Recent work has identified ways to use hardware transactional memory (HTM) to reduce descriptor allocation [9, 22]. Currently, HTM is supported only on recent Intel and IBM processors. Other architectures, such as AMD, SPARC and ARM have not yet developed HTM support. Thus, it is important to provide solutions for systems with no HTM support. Additionally, even with HTM support, our approach is useful. Current (and likely future) implementations of HTM offer no progress guarantees, so one must provide a lock-free fallback path to guarantee lock-free progress. The techniques in [9, 22] accelerate the HTMbased code path(s), but do nothing to reduce descriptor allocations on the fallback path. In some workloads, many operations run on the fallback path, so it is important for it to be efficient. Our work provides a way to accelerate the fallback path, and is orthogonal to work that optimizes the fast path.

The *long-lived renaming* (LLR) problem is related to our work (see [6] for a survey), but its solutions do not solve our problem. LLR provides processes with operations to *acquire* one unique resource from a pool of resources, and subsequently *release* it. One could imagine a scheme in which processes use LLR to reuse a small set of descriptors by invoking *acquire* instead of allocating a new descriptor, and eventually invoking *release*. Note, however, that a descriptor can safely be released only once it can no longer be accessed by any other process. Determining when it is safe to release a descriptor is as hard as performing general memory reclamation, and would also require delaying the release (and subsequent acquisition) of a descriptor (which would increase the number of descriptors needed). In contrast, our weak descriptors eliminate the need for memory reclamation, and allow immediate reuse.

#### 8 Conclusion

We presented a novel technique for transforming algorithms that throw away descriptors into algorithms that reuse descriptors. Our experiments show that our transformation yields significant performance improvements for a lock-free k-CAS algorithm. Furthermore, our transformation reduces peak memory usage by nearly three orders of magnitude over the next best implementation.

We also applied our transformation to a lock-free implementation of LLX and SCX, and studied its performance by doing rigorous experiments on a lock-free binary search tree that uses LLX and SCX. These experiments demonstrated a significant performance advantage for our transformed algorithm in workloads that perform many updates. Our transformed LLX and SCX algorithm has the potential to improve the performance of many algorithms that use LLX and SCX.

We believe our transformation can be used to improve the performance and memory usage of many other algorithms that throw away descriptors. Moreover, we hope that our extended weak descriptor ADT will aid in the design of more efficient, complex algorithms, by allowing algorithm designers to benefit from the conceptual simplicity of throwing away descriptors without paying the practical costs of doing so.

#### Acknowledgments

We thank Faith Ellen for her gracious help in proving correctness for our transformations, and her insightful comments. Some of this work was done while Trevor was a student at the University of Toronto, and while Maya was visiting him there. This work was supported by the Israel Science Foundation (grant 1749/14), the Yad-HaNadiv foundation, the Natural Sciences and Engineering Research Council of Canada, and Global Affairs Canada. Maya is supported in part by the Technion Hasso Platner Institute Research School.

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